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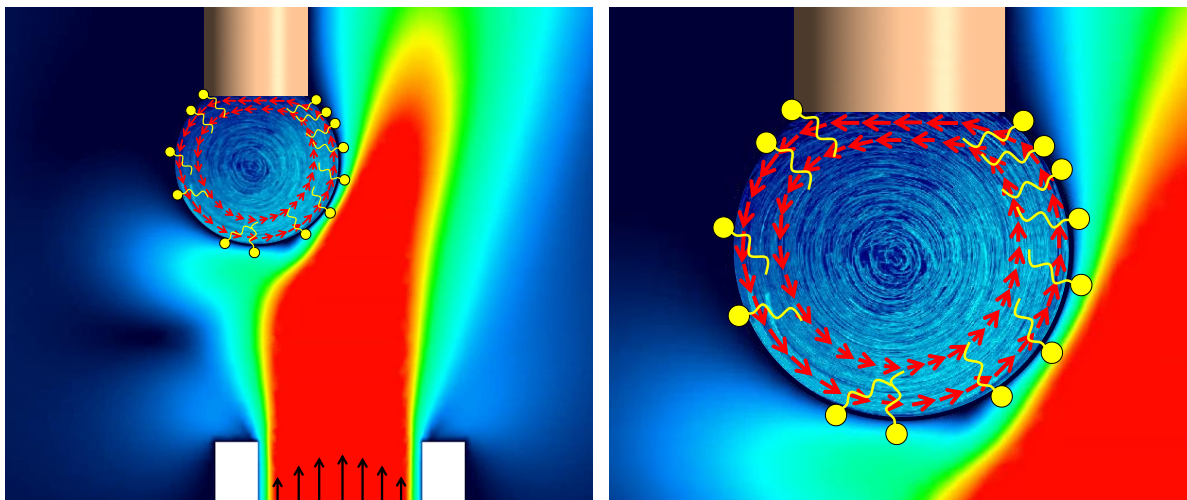
Interfacial flow of a surfactant-laden interface under asymmetric shear flow

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GRAPHICAL ABSTRACT



ABSTRACT

Hypothesis

The shear stress of the axisymmetric flow field triggers a nonuniform distribution of the surfactants at the surface of a rising bubble, known as stagnant cap. The formation of the stagnant cap gives rise to Marangoni stresses that reduce the mobility of the interface, which in return reduces the rising velocity. However, the conditions in technological processes usually deviate from the linear rise of a single bubble in a quiescent unbounded liquid. Asymmetric shear can act on the bubble surface e.g. due to the vorticity in the surrounding flow, bubble-bubble interactions, or influence of the reactor wall. A different surfactant distribution at the interface is expected under asymmetric shear, which can change the hydrodynamic behavior of the interface drastically.

Experiments

Here we conduct model experiments with a bubble or a drop at the tip of a capillary placed in a defined flow field. Thereby we investigate the influence of asymmetric shear forces on the interface in the presence of surfactants. Microscopic particle tracking velocimetry is employed to measure the velocity of the surfactant-laden interface for different degrees of asymmetry in the surrounding liquid flow.

Findings

We show a direct experimental observation of the circulating flow at the interface under asymmetric shear, which prevents the formation of the typical stagnant cap. Additionally, we reveal that the interface remains mobile regardless of the surfactant concentration. Our results confirm that increasing the degree of asymmetry increases the shear forces and thus the interfacial velocity.

1 1. Introduction

2 The adsorption of surface-active material at the interface changes the interfacial properties and
3 boundary conditions, and hence the interfacial mass and heat transfer rates ¹⁻³. Typically, the
4 adsorption process is considered instantaneous and the interface is supposed to be in equilibrium.
5 Yet, in practice, surfactant molecules require some time to (i) diffuse to the interfacial sub-layer
6 from the bulk phase, and (ii) to adsorb at the interface from the sublayer while (iii) adopting the
7 favored orientation ^{4,5}. Thus, understanding the dynamics of surfactant adsorption at the interface
8 is essential for the optimization and control of numerous industrial applications such as foams and
9 emulsions, material processing, pharmaceuticals, and cosmetics ⁶⁻⁹. Eastoe et al ¹⁰ and Miller et al
10 ¹¹ have provided a comprehensive review on the models developed to predict the equilibrium and
11 time dependent surface tension of surfactant solutions. Many of these models assume the interface
12 to be in quiescent condition. Yet, in view of technological applications, this assumption mostly
13 does not hold as convection takes place in the surrounding bulk phase and at the interface.
14 Therefore, in recent years, the emphasis has turned to moving interfaces and many studies have
15 been carried out to understand the behavior of interfaces under dynamic conditions ⁸⁻¹¹. Particularly
16 the interfacial dynamics of an air bubble rising in a liquid became an active research area ¹⁶⁻¹⁸ due
17 to its high relevance to natural and industrial processes. It was shown that the surfactant adsorption
18 rate ¹² as well as its distribution at the interface ¹⁹ changes significantly in presence of flow. At the
19 surface of a rising bubble, a nonuniform interfacial concentration distribution develops due to the
20 surface advection caused by the main flow. The interfacial concentration gradient creates a
21 tangential stress known as Marangoni stress, which opposes the shear stress of the flow ³. At
22 sufficiently high surfactant concentrations, the Marangoni stress retards the surface motion and
23 thereby ceases the internal circulation known as Hadamard-Rybczynski flow ²⁰. The
24 immobilization of the interface increases the drag coefficient towards that of a rigid sphere ²¹ and
25 likewise forces the terminal velocity of the bubble to approach that of a rigid sphere ^{13,22,23}. To
26 reflect the transition from mobile to immobile interface, the stagnant cap model is typically used
27 in the literature. This simplified model divides the bubble interface in a fully immobile part at the
28 trailing edge where the cap angle grows with increasing interfacial concentration, while the leading
29 edge of the bubble remains mobile.

30 However, to describe the adsorption-desorption kinetics of a moving interface in more refined
31 models, one needs to quantify the molar fluxes of the surfactant to and at the interface. This requires
32 an accurate velocity measurement at the interface and its boundary layer, which would further
33 allow a proper characterization of large variety of phenomena, such as bubble migration and
34 accumulation, connected with the shear-induced lift force on bubble motion ²⁴. Even for a spherical
35 bubble with clean surface rising in a linear shear flow, the influence of different parameters such
36 as the Reynolds number, and the presence of walls leads to a nontrivial dependence of the lift
37 coefficient ²⁵. In case of contaminated bubbles, the shear flow will also interact with the surfactant
38 distribution on the interface, yielding additional complexity. Likewise, surface deformations,
39 bubble-bubble interactions and Marangoni stresses at the interface lead to a high degree of

1 interaction that requires comprehensive experimental and/or numerical methods to identify the
2 driving mechanisms and quantitative correlations. Takagi and Matsumoto²⁴ reviewed recent
3 observations on the effect of adsorbed surfactants on the migration of bubbles in shear. Takagi et
4 al²⁶ found that in the absence of surfactant, the bubbles tend to move toward the channel center.
5 However, in presence of a small amount of surfactant, the bubbles tend to move toward the wall.
6 They further confirmed that increasing the surfactant concentration increases the Marangoni
7 stresses, so that the bubbles are shifted toward the center of the channel again. Due to the
8 asymmetric shear forces acting in these cases, a surfactant distribution different from the symmetric
9 stagnant cap model can be expected^{27,28}, which can change the boundary conditions around the
10 bubbles significantly. As mentioned, a precise measurement of the velocity field would allow
11 unraveling the above-described complex phenomena. However, the optical methods that are used
12 to record the velocity distribution in the bulk fluids usually are lacking the spatial resolution to
13 fully capture the boundary layer and thus the interfacial flow. Hosokawa et al.¹⁵ evaluated the
14 surface concentration profile of a falling drop using spatiotemporal filter velocimetry, giving access
15 to the velocity field near the interface. Nevertheless, the interfacial velocity needs to be
16 extrapolated from the closest velocities measured. This can introduce considerable uncertainties to
17 the calculated data because of high velocity gradients in the boundary layer. Besides, such
18 techniques are mostly limited to fluid-fluid interfaces since a high accuracy requires matching the
19 refractive index of both phases.

20 In this study, direct experimental insights in the behavior of bubble and droplet interfaces under
21 asymmetric shear forces are provided to address the above-sketched deficits. To that end, a
22 reference flow is created around a stationary bubble placed at the tip of a capillary. This reference
23 flow can be tuned with respect to the degree of asymmetry to impose different shear rates on the
24 bubble surface. Particle image velocimetry (PIV) coupled with particle tracking velocimetry (PTV)
25 is applied to characterize the flow around the bubble as well as on its surface. By tracking the
26 adsorbed tracer particles, the interfacial flow can be captured with high spatial and temporal
27 resolution. This method eliminates the uncertainty linked with the extrapolation of the boundary
28 layer velocity, as the velocity at the interface can be directly measured by tracking the adsorbed
29 particles movement at the interface. Profile analysis tensiometry (PAT) was conducted to study the
30 interfacial properties of the employed surfactant. In combination with the measured velocities, the
31 hydrodynamic shear stress on the interface is evaluated and further used to estimate the Marangoni
32 stress, interfacial tension, and surfactant concentration distribution at the interface.

33 Our results indicate that the surrounding asymmetric velocity field creates a defined rotational
34 flow at the bubble surface, which increases with the degree of asymmetry. This further changes the
35 distribution of the surfactants at the interface. More importantly, our results demonstrate that under
36 asymmetric shear flow, the interface remains *mobile* regardless of the concentration of the added
37 surfactant. This phenomenon is expected to have significant influence on the hydrodynamics and
38 mass transfer at bubbles with adsorbed material in various processes in chemical and minerals
39 engineering.

1 2. Materials and methods

2 2.1. Liquids

3 Ultrapure water (Milli-Q ELGA, United Kingdom) with 18.2 M Ω resistivity and < 2 ppb organic
4 content is used to prepare the aqueous solutions. Glycerol (CHEMSOLUTE, Germany) with a
5 purity of $\geq 99.5\%$ and silicone oil (Sigma Aldrich, Germany) were used to prepare refractive
6 matched fluids.

7 In optical measurements, matching the refractive index of a two-phase system minimizes the
8 distortions by the light refraction at the phase boundaries and hence increases the accuracy of the
9 measurements ²⁹. Liquid-liquid combinations with a refractive index around 1.4 are commonly
10 used in the literature, as this value is easy to implement for several aqueous-organic systems by
11 adding the corresponding amount of glycerol to water. For the silicone oil used in this study, a
12 matching refractive index between both phases was found at 49.3 wt% glycerol. A digital
13 laboratory refractometer (LR-01, Maselli, Italy) was employed to measure the refractive index of
14 the employed liquids accurately. Table 1 shows the physical properties of the pure liquids and the
15 water-glycerol mixture.

Table 1. *Liquids used in experiments, with their refractive index, density, and viscosity at room temperature.*

	Water	Glycerol	Silicone Oil	Water-Glycerol
Refractive index	1.33272	1.47240	1.39629	1.3959
Density (kg·m ⁻³)	998	1231	913	1125*
Dynamic viscosity (mPa·s)	1.04	1420	4.6	4.9*

* the values are adopted from Sheely et al ³⁰.

16 2.2. Surfactants

17 Sodium dodecyl benzene sulfonate (SDBS, anionic surfactant) with a purity of $\geq 99\%$ was used
18 as purchased (Merck, Germany). The anionic surfactant was chosen to avoid unwanted
19 hydrophobization of the tracer particles for the flow measurements, which would be expected in
20 the case of cationic surfactants due to the electrostatic adsorption of cationic surfactants on the
21 negatively charged surface of the particles ³¹. The critical micelle concentration (CMC) value of
22 SDBS was determined by surface tension measurements. The results provided a CMC value of 2.2
23 mM, which is in good agreement with the literature value ³².

24 2.3. Surface tension

25 Profile analysis tensiometry (PAT-1M, Sinterface Technology, Germany) was used to evaluate
26 the dynamic surface tension of the employed solutions. The principle of measurement is described
27 in detail in ³². Briefly, a drop is created at the tip of a stainless-steel capillary. The pear-shaped
28 profile of the pendant drop is defined by the interaction of interfacial tension and gravity. Using
29 image processing, the droplet profile is determined and fitted by the Gauss-Laplace equation and
30 from that, the interfacial tension is obtained.

2.4. PIV measurements

Particle image velocimetry (PIV; LaVision, Germany) was applied to measure the flow around the bubble and on its surface. PIV is an optical technique to measure the velocity field in a fluid that is seeded with sufficiently small and neutrally buoyant tracer particles. Polystyrene (PS) particles (microParticles GmbH, Germany) with a diameter of 5.06 μm , a density of 1020 $\text{kg}\cdot\text{m}^{-3}$ and an incorporated fluorescent dye (rhodamine; red fluorescent: excitation and emission at 530 nm resp. 607 nm wavelength) served as tracers. At low Stokes numbers, the particles follow the movement of the fluid perfectly³³. The Stokes number for the particle-laden flow around the bubble is defined as:

$$\text{St} = \frac{\rho_p D_p^2 u_{\text{Max}}}{18 \mu_f D_b} \quad (1)$$

where ρ_p is the density of the particle, D_b and D_p are bubble and particle diameters, respectively, u_{Max} is the maximum velocity present within the system (for a conservative estimation), and μ_f is the dynamic viscosity of the fluid. The Stokes number in our case was $\text{St} \approx 0.01 \ll 1$ suggesting the high ability of the particles to follow the flow. Excited by a Nd-YLF laser (Photonics Industries, USA), the fluorescent particles emit light that is separated from the background scattered light of the laser by an optical long-pass filter. Thereby, mainly the particle signal is captured by the high-speed camera (Phantom VEO 410L, 1280 \times 800 pix, AMETEK, USA) via a Zeiss Stereo microscope with PlanApo S 1.0 \times objective (Zeiss, Germany), used at 3.2 x zoom level. These optical parameters yield a spatial resolution of ~ 250 px/mm. The temporal resolution of the high-speed camera was set to 200 fps. Due to the confocal optics, the tracer particles are imaged sharply in a quasi-2D measurement plane (depth of field 0.18 mm) while the blurred signals outside the measurement plane do not contribute to the evaluation algorithm. This algorithm divides the recorded images in discrete interrogation windows that set the spatial resolution of the vector field. The movement of the tracer particles in the interrogation windows is determined from the cross-correlation of two consecutive images. This relatively coarse velocity field serves as a predictor for the velocity distribution. Subsequently, particle tracking velocimetry (PTV) is applied as post processing to individual tracer particles to achieve higher spatial resolution within the interrogation window (PIV evaluation software DaVis, LaVision, Germany)³⁴. PTV was also employed for tracer particles adsorbed on the bubble surface to study the interfacial flow.

The setup to create the flow around a bubble is similar to that reported previously by Lotfi et al¹². A cuvette with a cross-sectional area of 30 \times 30 mm^2 and a height of 30 mm was mounted on top of a translation stage (labelled in Fig. 1a). As shown by the detail in Fig. 1b, the bubble was formed at the tip of a straight capillary (outer diameter 1.2 mm) using a micro syringe (for this precise dosing, the volumetric control of the afore-mentioned PAT-1M device was also utilized here). A steady liquid flow from the bottom to the top of the cuvette was generated using a U-shaped capillary of ~ 2 mm inner diameter as a nozzle which was connected to a syringe pump (Ascor med, Poland; labelled in Fig. 1a). The composition of the inflowing liquid is identical to the liquid in the cuvette. The vertical distance between the inlet nozzle and the bubble was set to $\Delta h = \sim 7$ mm. The end part of the U-shaped capillary points vertically towards the bubble center and can be shifted in

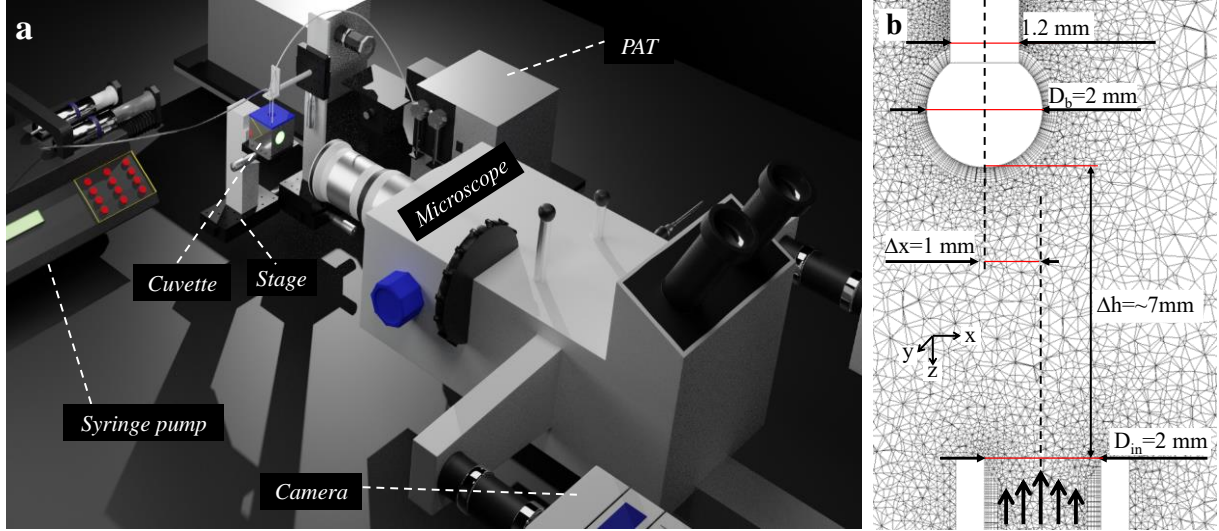


Figure 1. a) Stereo PIV setup to measure the velocity field. b) Mesh used for the simulations inside the *cuvette* (a) together with definition of the geometry with a bubble at the end of a capillary placed above the flow of the inlet nozzle.

1 x-direction by means of the translation stage, setting a horizontal distance of Δx between the
 2 centerline of the bubble and that of the inlet nozzle (cf. Fig. 1b). For laminar flow inside a pipe, the
 3 entrance length (L_e) can be calculated using equation 2:

$$4 \quad \frac{L_e}{D_{in}} = 0.06 \text{Re}_{\text{pipe}} \approx 1.8 \quad (2)$$

5 where D_{in} is inner diameter of the pipe, and Re_{pipe} is the Reynolds number of the flow inside the
 6 pipe. The straight end part of the U-shaped capillary in our experiments was more than $2D_{in}$; hence,
 7 a fully developed flow is expected inside the inlet nozzle.

8 2.5. Numerical simulations

9 3D numerical simulations of the flow field around a bubble placed on the tip of a capillary were
 10 carried out using the *commercial software* ANSYS CFX. It solves the unsteady Navier-Stokes
 11 equations on structured or unstructured meshes employing the finite volume method. The
 12 numerical setup and the mesh are shown in Fig. 1b. Due to the low bubble Reynolds number of
 13 approximately 20, a steady-state isothermal simulation without turbulence modeling is performed.
 14 Around the bubble, an inflation layer with radial resolution equal to $10^{-5} \text{ m} = 0.01 R_b$ and growth
 15 rate, equal to 1.2 was generated. The growth rate represents the increase in mesh size with each
 16 succeeding layer, starting from a defined face, in this case the bubble surface. For example, a
 17 growth rate of 1.2 results in a 20% increase in mesh size with each succeeding layer. A constant
 18 mass flow rate was imposed at the inlet. The same mass flow rate was set at the upper boundary to
 19 mimic a rising water level. The bubble surface adopted either a boundary condition with no-slip
 20 and zero velocity (corresponding to a solid sphere) or free-slip (corresponding to a perfectly clean
 21 bubble), while all other boundaries were kept no-slip. Additionally, the bubble surface is assumed
 22 undeformable in numerical studies, which is line with the experimental observation, i.e. absence of

1 deformations at employed flow rates. Indeed, in higher flow rates, the bubble deformation due to
 2 the dynamic pressure from the flow needs to be considered. A mesh sensitivity analysis was
 3 performed to check the convergence of the simulations. The results showed that the velocity
 4 magnitude close to the bubble surface changes in average less than 1% by doubling or halving the
 5 grid size. For this estimation, the velocity magnitude variation at 100 points is considered, which
 6 were homogenously distributed between R and $1.25R$. Additionally, the net torque on bubble
 7 surface changed less than 1% by changing the mesh.

8 3. Results and discussion

9 3.1. Surface tension

10 To characterize the interfacial properties of the employed surfactant SDBS, the equilibrium
 11 surface tension values are measured as a function of surfactant concentration using the pendant
 12 drop method (PD). Fig. 2a shows the obtained isotherm for SDBS. The isotherm is used to calculate
 13 the amount of adsorbed material at the interface, the CMC value, and the partial molar area of the
 14 surfactant^{32,35,36} which will be needed in Sec. 3.4. Indeed, it would appear more logical to use a
 15 buoyant bubble (BB) instead of a PD to have better analogy with the previously described PIV
 16 setup. However, because of the following practical advantages the PD method is employed. The
 17 fitting of the buoyant bubble profile to the Gauss-Laplace equation (cf. Sec. 2.3) is more
 18 challenging due to the accuracy limit on the edge detection of a bubble image^{37,38}. More
 19 importantly, the BB technique is much more susceptible to the influence of impurities within the
 20 system due to the direct contact of the studied liquid with the container. On the other hand, PD
 21 normally delivers a higher equilibrium surface tension values at the same surfactant concentration
 22 because of the known depletion effect. Due to the limited amount of surfactant available in the
 23 droplet volume, the bulk concentration of the system decreases as the surfactant adsorbs at the
 24 interface³⁹. The depletion effect can be quantitatively addressed via a mass balance:

$$25 \quad c = c_0 - (sur/vol)\Gamma \quad (3)$$

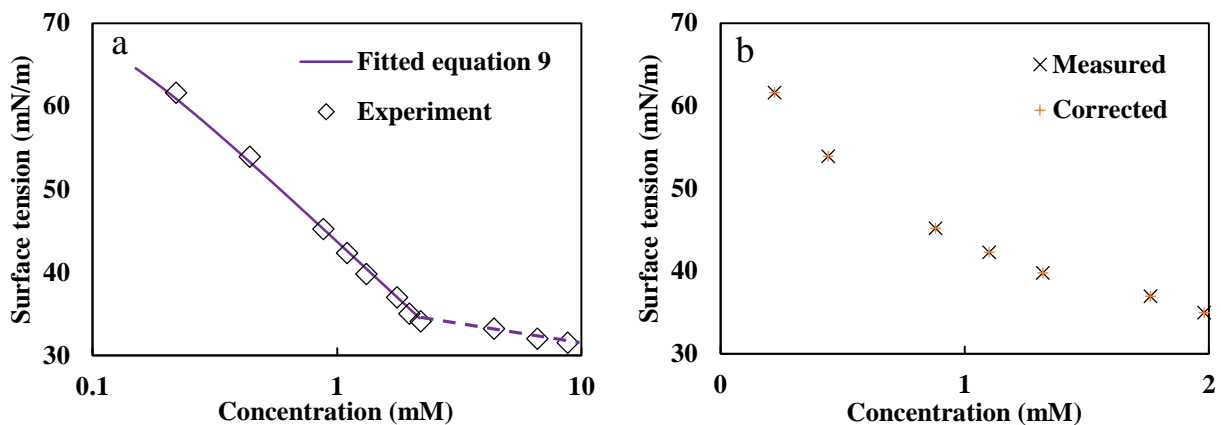


Figure 2. a) Equilibrium surface tension as a function of SDBS concentration measured using the pendant drop method (PD). The dashed line for $C > 2.2$ mM is drawn as guide for the eye. b) Comparison between the measured and corrected isotherms for SDBS considering the depletion effect.

1 where c and Γ are the bulk and surface concentration of the surfactant, respectively, sur is the area
2 of the interface, and vol is the volume of the phase that contains the surfactant. The second term at
3 the right-hand side of equation 3 expresses the concentration decrement in the bulk due to the
4 surfactant adsorption.

5 As can be inferred from equation 3, the depletion effect is much more prominent for the PD
6 method as the surface area to volume ratio is much higher compared to the BB method. Therefore,
7 the PD results were corrected using equation 3 and the corrected values are plotted in Fig. 3b. As
8 one can see from this figure, the surface tension values are almost identical for the employed
9 surfactant and the depletion effect can be neglected.

10 3.2. Flow field around the bubble

11 Flow-on-bubble experiments allow exerting a defined shear on the bubble surface merely by
12 shifting the relative position of the bubble to the inflow jet. Additionally, this setup allows adjusting
13 relevant parameters independently, such as bulk velocity, bubble size, and surfactant concentration.
14 In rising bubble experiments, by contrast, the terminal velocity at constant bubble size decreases
15 with increasing surfactant concentration⁴⁰. For our experiments, a defined and reproducible flow
16 field was generated using the setup depicted in Fig. 1. The volumetric flow rate was set to 150
17 mL·h⁻¹ corresponding to a bulk velocity of ~13.3 mm·s⁻¹ directly at the nozzle outlet. The flow
18 measurements were carried out in an aqueous solution containing different concentrations of
19 SDBS, varied the range of 0.22 mM to 8.8 mM. However, no clear effect of the surfactant
20 concentration on the flow pattern was observed for the range of surfactant concentrations employed
21 in this study. Hence, we focus on a concentration of 2.2 mM, corresponding to CMC, and provide
22 exemplary results throughout the whole concentration range in the SI (cf. Figure S1). This high
23 surfactant concentration was chosen (i) to account for the large amount of surface-active materials
24 present in many industrial processes and (ii) to minimize the influence of unwanted impurities from
25 setup parts and/or the surrounding atmosphere. It is worth mentioning that a slight dissolution of
26 the fluorescent dye from the PS tracer particles already can introduce a certain degree of
27 contamination to the system, which can affect the interfacial hydrodynamic properties of an
28 otherwise pure system⁴¹. It should be noted that the bubble surface reaches the equilibrium quite
29 fast for concentrations around CMC. Additionally, the presence of flow significantly increases the
30 adsorption rate¹² and one can assume that the interface has approached equilibrium in the time
31 between switching on the flow and starting the PIV measurement.

32 Because of the rather specific geometry of the studied system, the velocity field is thoroughly
33 characterized by a combination of PIV measurements and numerical simulations on a similar setup
34 (cf. Fig. 1b). The simulations further allow estimating 3D parameters of the flow such as the total
35 torque on the bubble surface. Fig. 3 compares the numerical no-slip (a,c) and experimental (b,d)
36 results for a bubble placed centered (a,b) and off-centered (c,d) with respect to the inlet nozzle for
37 2.2 mM of SDBS. The experimental data is time-averaged over 2 s. In the case of a symmetric flow
38 around the surfactant-laden bubble, a stagnation point on the leading edge and a pronounced wake
39 (blue region of low velocity) on the trailing edge of the bubble are visible. Since the nozzle provides
40 a jet rather than a homogeneous flow field, the flow is forked by the bubble, leading to an earlier
41 detachment of the flow at the bubble perimeter and a more prominent wake. Rising bubbles present

1 a concentration gradient of adsorbed substances along their surface due to the surface advection
 2 caused by the main flow. Such a nonuniform distribution of surfactants causes a surface tension
 3 gradient that triggers a Marangoni stress opposing the shear stress of the flow. An analogous effect
 4 might be expected for a bubble on the tip of a capillary placed in a symmetrical flow. In this case,
 5 a surfactant rich area would develop close to the capillary and a “clean” interface at the leading
 6 edge of the bubble. In Fig. 3, the experimental results are reproduced well by the simulations with
 7 a no-slip bubble surface. This is indicated by the regions of near-zero velocity adjacent to the
 8 bubble surface in the experiment which are absent for a free-slip surface (cf. SI, Figure S2). Since
 9 a similar flow field was obtained for all employed surfactant concentrations, we conclude that a
 10 no-slip boundary condition was reached in each case. This agrees with the observations from
 11 Hosokawa et al ^{2,15} who have reported a nearly retarded interface in presence of only 0.036 CMC,
 12 i.e. 10^{-2} mM of a Triton surfactant.

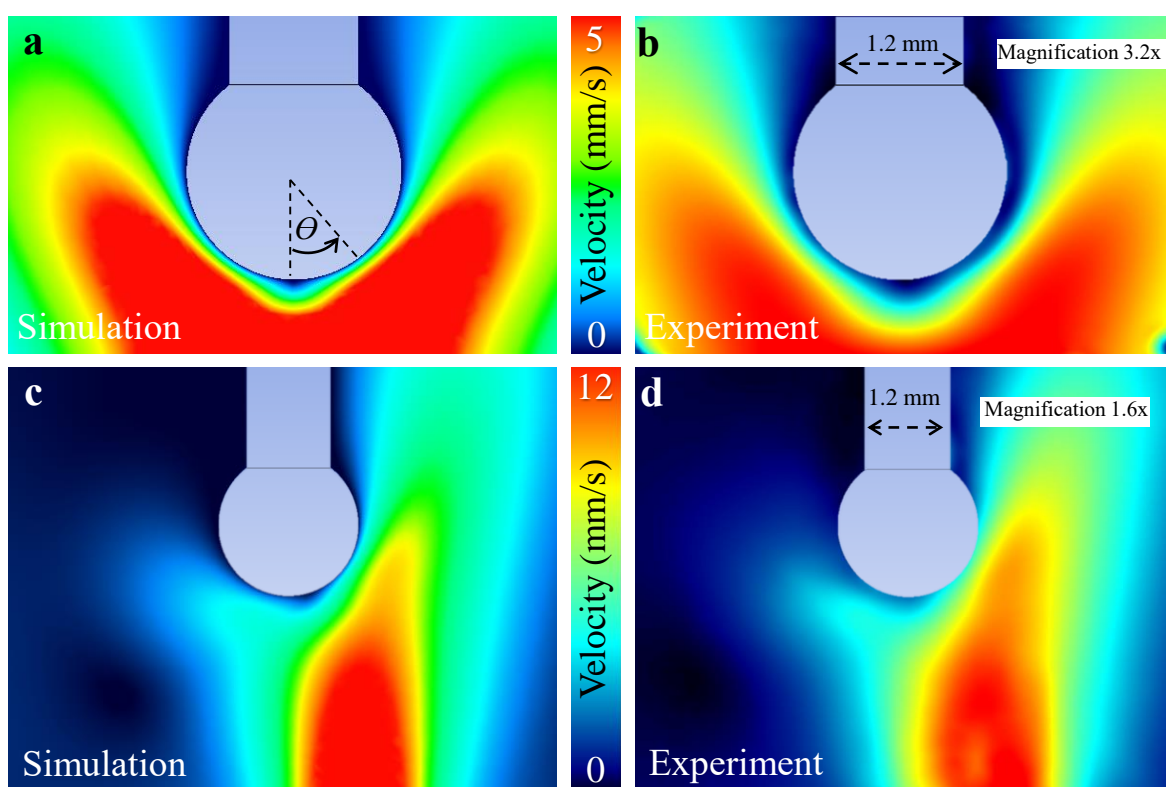


Figure 3. Velocity distribution around a bubble attached to the tip of a capillary for experiments with 2.2 mM SDBS and simulations with no-slip surface boundary condition. a,c) Simulation (ANSYS, steady state) and b,d) experiment (time-averaged over 2s); a,b) 3.2 x magnification and symmetric position with respect to inflow; c,d) 1.6 x magnification with 1 mm asymmetric position (Δx according to the definition in Fig. 1b).

13 To study the behavior of the bubble surface under asymmetric shear, we now shift the bubble in
 14 horizontal direction (cf. Fig. 1b). Thus, the center of the inflow with maximum velocity is located
 15 at the bubble side, here with a displacement of 1 mm. The good agreement between the flow pattern
 16 of the experiment and the simulation again suggests that the system yields a flow boundary

1 condition that is close to no-slip (cf. Fig. 3 c,d). However, the region with zero velocity adjacent to
 2 the bubble surface is not clearly visible at the right-hand side of the experimental velocity field.
 3 This can be attributed to experimental uncertainties or the existence of a slow interfacial flow in
 4 the asymmetric case, which can also cause a certain deviation from the theoretical no-slip case.

5 3.3. Interfacial flow on the bubble surface

6 The response of the interface to the asymmetric shear flow is studied by tracking the adsorbed
 7 PS particles at the bubble surface (example videos V1.mp4 and V2.mp4 in SI). Fig. 4a illustratively
 8 shows how the adsorbed particles move in response to the asymmetric shear flow. The bulk velocity
 9 difference between the left and the right side of the bubble drives a rotational surface flow. This
 10 surface flow is aligned with the bulk flow on the right side, where the bulk velocity is higher. On
 11 the left side of the bubble, where the bulk flow is slower, the interfacial flow opposes the bulk flow
 12 direction by pointing downwards. Irrespective of the interfacial flow, one might argue that the
 13 particles are dragged upward by viscous forces on the right-hand side and move downward on the
 14 left side by inertia. However, the negligible density difference between the PS particles and the
 15 aqueous solution as well as the low particle Stokes number (equation 1) demonstrate that the
 16 particles should follow the streamlines of the flow nearly perfect. Consequently, inertia effects
 17 cannot explain the movement of the PS tracers. To reconstruct the three-dimensional movement of
 18 the PS particles, we use the information that the PS particles are bound to the interface. By
 19 describing the bubble surface as a spheroid (equation 4), the out of plane component of the velocity
 20 V_y can be derived from the position (x, z) and velocities (V_x and V_z) of the two-dimensional images.
 21 Since the velocities in x and z direction are both known from the PTV evaluation, the third velocity
 22 component is calculated according to equation 5.

$$23 \quad \frac{x^2}{a^2} + \frac{y^2}{a^2} + \frac{z^2}{b^2} = 1 \quad (4)$$

$$24 \quad V_y = -\frac{xV_x + \frac{a^2}{b^2}zV_z}{y} \quad (5)$$

25 An example for the obtained 3D path of a well-visible cluster of PS particles is shown in Fig. 4a
 26 and b where the velocity of the cluster approximately represents the interfacial velocity. Interaction
 27 and agglomeration of the adsorbed tracer particles certainly influence the direct coupling of the
 28 particle movement to the interfacial flow. However, the phenomenon of rotating flow remains
 29 unchanged when the seeding with tracer particles is sparser.

30 The velocity components normalized by the inlet velocity are plotted in Fig. 4c-e over the angular
 31 position θ (defined in Fig. 3a). The depicted particle path starts at $\theta \approx -40^\circ$ (start position marked
 32 green) and after approx. 0.5 seconds, the particles reach the leading edge of the bubble ($\theta = 0^\circ$).
 33 Driven upwards by the surface flow, they approach the position of the capillary. Like a two-
 34 dimensional flow around a cylinder, the capillary poses an obstacle and a stagnation zone forms in
 35 front of the capillary. Consequently, all velocity components strongly decrease near the capillary
 36 $|\theta| > 140^\circ$. Thereafter, the particles either can be trapped in the stagnation zone to form a large
 37 stationary particle agglomerate or – depending on their position – are reaccelerated to another

- 1 circulation on the bubble surface. Additionally, the circulating movement is disturbed by the needle
- 2 resulting in a redistribution of the particles on the surface.

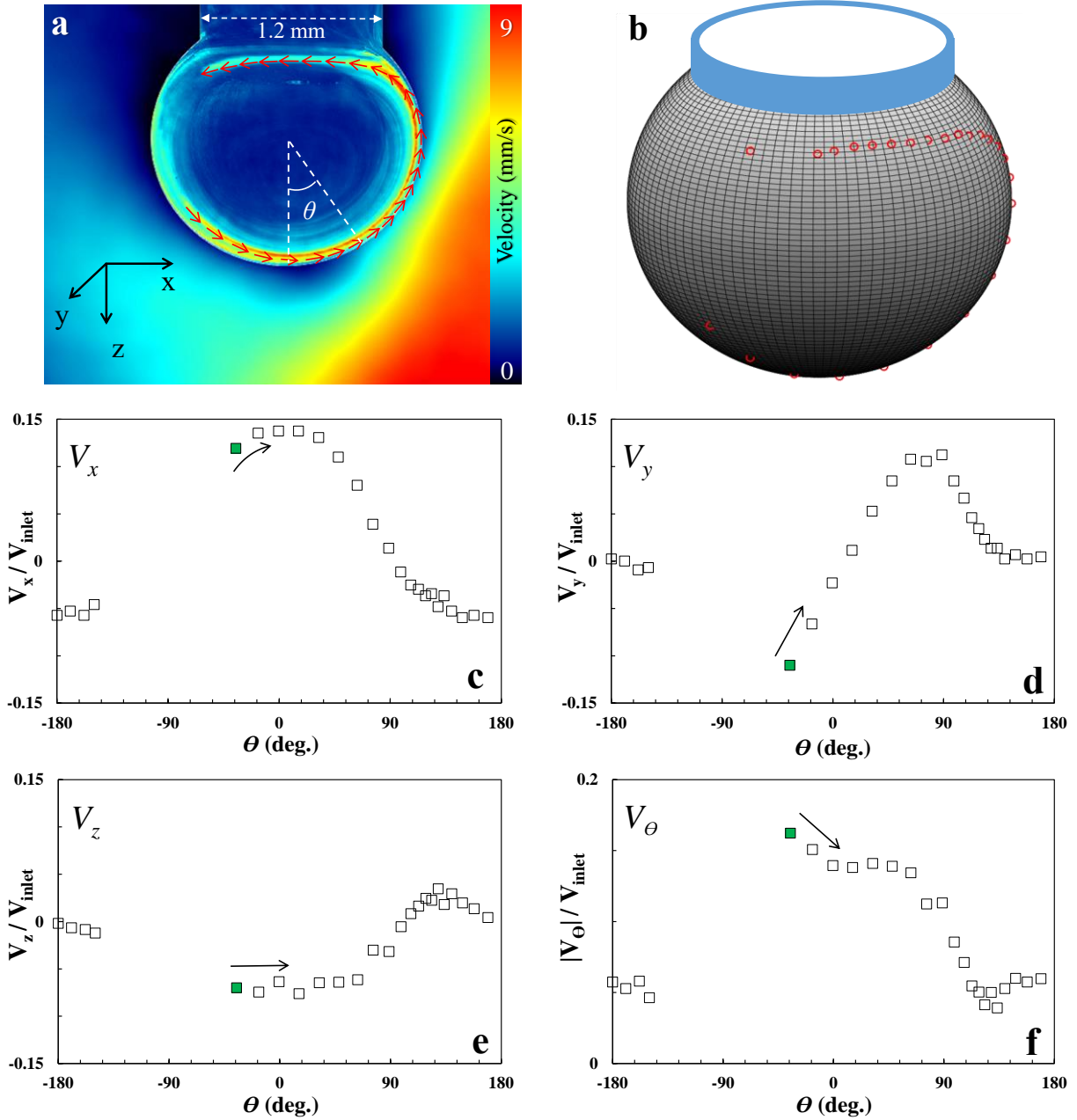


Figure 4. a) Particle movement at a bubble surface subjected to shear flow. b) Reconstructed 3D path of particles using equations 4 and 5. c)-f) Velocity components of the same particle group as a function of the polar angle θ .

- 3 In the next step, the effect of asymmetry on the rotational velocity of the interface is investigated.
- 4 It is worth noting that the interfacial velocity is not constant at the bubble surface (c.f. Fig 4f).
- 5 Hence, the speed of revolution ($\bar{\omega}$) is calculated as an average value, indicating the time required
- 6 to complete at least one cycle of 2π . For asymmetry levels below 0.2 mm, $\bar{\omega}$ was too low to
- 7 complete a cycle within the time of measurement; hence, we consider only the data for $\Delta x \geq 0.2$

1 mm. Fig 5 (violet squares) shows $\bar{\omega}$ of the particles at the interface (representing the velocity of the interface) as a function of the asymmetry. As can be seen from this figure, $\bar{\omega}$ increases with increasing asymmetry. Since the bulk flow structures between the experiments and simulations agreed well (cf. Sec. 3.2), we use the numerical results to calculate the net torque (Ω) (Fig. 5, unfilled triangles). This is the torque in y-direction, exerted by the liquid flow field onto the bubble surface, integrated over the full bubble surface. This quantity is not accessible in the experiments, because the employed PIV method does not capture the full three dimensional flow field around the bubble simultaneously. The net torque Ω was further employed to estimate the theoretical value of $\bar{\omega}$ for the bubble. The theoretical angular velocity (ω) of a solid sphere of radius R_s rotating in a quiescent fluid with viscosity μ_f is given in ⁴².

$$11 \quad \Omega = 8\pi\mu_f R_s^3 \omega \quad (6)$$

12 Comparing this relation with our numerically calculated net torque yields a theoretical speed of revolution that is plotted in Figure 5 as well. Although the speed of revolution increases with the level of asymmetry in both experiment and simulation, the experimental $\bar{\omega}$ values are significantly smaller than the theoretically estimated ones (ω). Beside the slight differences in the bulk flow field, the deviation presumably results from three contributions. Firstly, the capillary prevents the free rotation underlying equation 6. Secondly, despite the low Reynolds number in the order of 1, the nozzle flow and the solid body rotation flow might not be perfectly superpositionable. Thirdly, the bubble interface does not act as a solid body but has fluidic/elastic properties.

20 3.4. Estimation of shear stress and surface concentration of surfactant

21 To shed light on the mechanisms underlying the observed interfacial flow, we investigate the shear stress and the concentration distribution on the bubble surface. For that purpose, the tangential velocity component V_θ at the bubble surface and at its boundary layer is extracted from the PTV/PIV measurements. The surface velocity is known from the tracking of adsorbed particles at the bubble surface (cf. Fig. 4) and the boundary layer velocity denotes the closest bulk PIV velocity vector adjacent to the bubble surface. Fig. 6a shows the surface velocity over the polar angle θ for 1 mm asymmetry in presence of 2.2 mM SDBS. Note, that this investigation does not consider the complete three-dimensional interface of the bubble but only the center plane ($y=0$) of the bubble. Here, positive values point in counterclockwise direction. Since the PIV measurements focus on the $y=0$ plane, we proceed with a two dimensional analysis. The gradient of V_θ at the bubble surface in normal direction is coupled to the tangential shear stress τ_θ

$$32 \quad \tau_\theta \Big|_{r=R_b} = \mu_f r \frac{\partial(V_\theta/r)}{\partial r} \Big|_{r=R_b} \quad (7)$$

33 where $\partial V_\theta/\partial r$ is approximated by the difference of the surface velocity to the closest bulk PIV velocity and their normal distance. The shear stress τ_θ at the interface (for the $y=0$ plane) is depicted in Fig. 6b (open squares) and compared to the wall shear stress from the corresponding simulations of a solid sphere at a needle tip (plus sign).

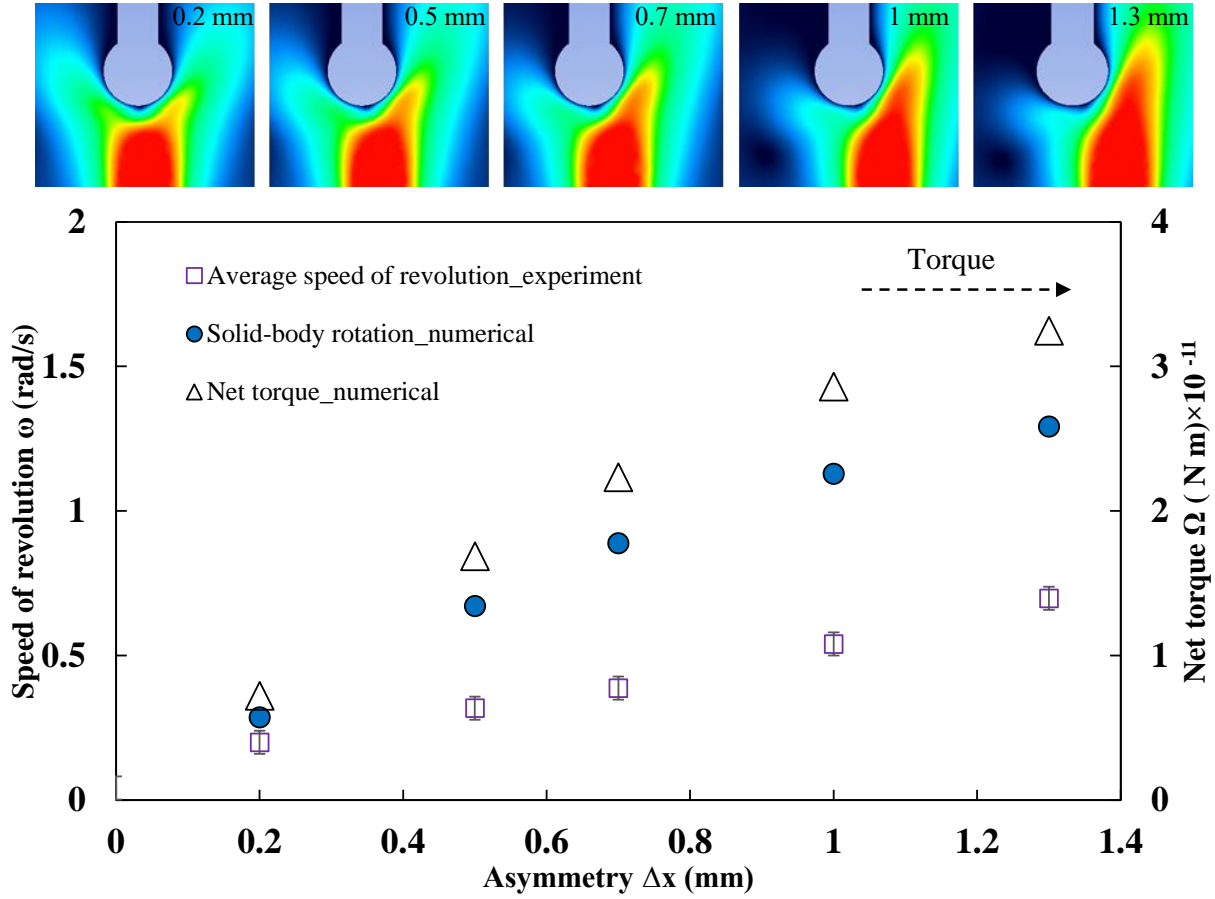


Figure 5. Speed of revolution as a function of asymmetry for an air bubble under shear flow. The solid-body angular velocity (ω , blue circles) was obtained using Eq. (6). The error bars estimate the variation of the speed of revolution between independent experimental runs. The top row of Fig. 5 shows the numerical flow field for each asymmetric configuration.

1 Fig. 6b displays two further simulations: the same asymmetric jet flow is exerted on a static solid
 2 sphere without needle (black crosses) and on a solid sphere with imposed constant rotation equal
 3 to $\omega=0.5 \text{ rad}\cdot\text{s}^{-1}$ (blue circles). As one can see, the shear stress for the stationary sphere is almost
 4 identical to the one with capillary because the capillary is placed in the wake of the flow where the
 5 velocities are almost zero. For the rotating sphere, the magnitude of the imposed velocity is adapted
 6 from the experimental results, i.e. $\omega \approx 0.5 \text{ rad}\cdot\text{s}^{-1}$ for 1 mm asymmetry (see Fig. 5). As can be seen
 7 from Fig. 6b, the rotation only leads to slight differences in the wall shear stress. This again
 8 emphasizes that the slow rotation observed in the experiment does not change the wall shear stress
 9 considerably. Hence, the order of magnitude of the torque that has been calculated numerically
 10 should be within the range of the experiment.

11 Finally, to estimate the concentration distribution of the adsorbed surfactant on the interface
 12 along the center plane ($y=0$), we employ the Marangoni shear stress balance

$$13 \quad \tau_\theta = \frac{1}{R_b} \frac{\partial \sigma}{\partial \theta}. \quad (8)$$

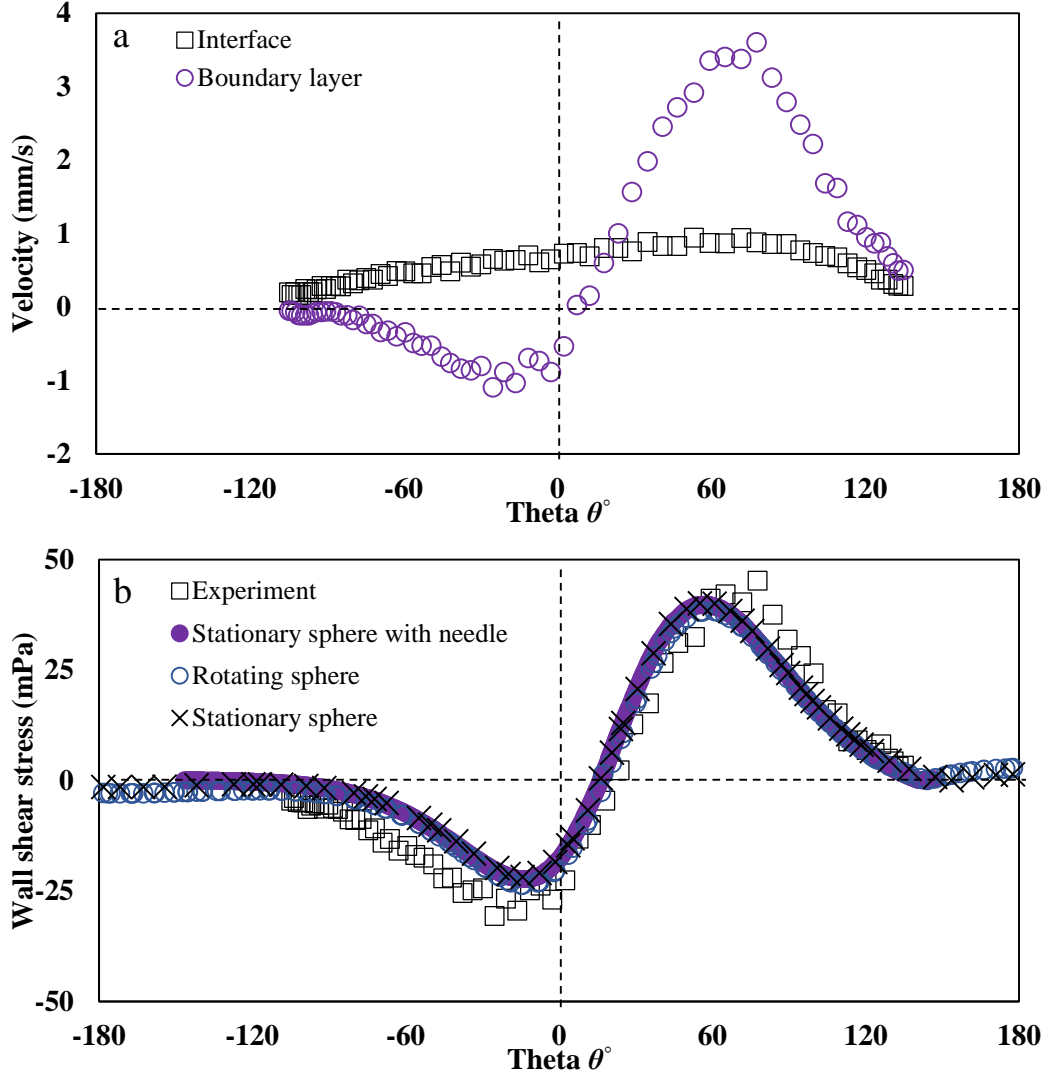


Figure 6. a) Tangential velocity distribution at bubble surface and its boundary layer for 1 mm asymmetry level. b) Wall shear stress is calculated from experimental velocity measurements using equation 7 and results of Fig. 6a, and from corresponding simulations of a solid sphere in an asymmetric flow field resting static on a needle (plus), resting static without needle (cross), and rotating ($0.5 \text{ rad}\cdot\text{s}^{-1}$, circle)

1 This equation assumes that the hydrodynamic stress is compensated by the Marangoni stress arising
 2 from the distribution of the surfactants at the interface. For a clean interface, there is no surface
 3 tension gradient and the surface flow follows the bulk flow. Thus, τ_θ must be zero, which is the
 4 above-mentioned condition for free-slip boundaries. Equation 8 has been widely used in the
 5 literature to calculate the distribution of surfactants at interfaces^{13,14,43–46}. Once the dependence of
 6 σ on Γ is established, the surface concentration can be calculated using equations 7 and 8.
 7 According to Butler's equation, the surface tension relates to the bulk concentration as follows³²:

$$8 \quad \sigma_w - \sigma = \frac{\bar{R}T}{a} \ln \left[1 + \frac{c^2}{4CMC^2} \exp \left[\frac{a}{\bar{R}T} (\sigma_w - \sigma_s) \right] \right] \quad (9)$$

1 where σ , σ_w and σ_s are the surface tension of surfactant solution, water and pure surfactant,
 2 respectively, a is the maximal partial molar area and CMC is the critical micelle concentration of
 3 the surfactant, \bar{R} is the universal gas constant and T is the absolute temperature. The Gibbs
 4 isotherm for the surface concentration of ionic surfactants reads

$$5 \quad \Gamma = -\frac{1}{2\bar{R}T} \frac{\partial \sigma}{\partial \ln c}. \quad (10)$$

6 Employing equations 9 and 10, equation 8 reduces to:

$$7 \quad \tau_\theta = \frac{1}{R_b} \frac{\partial \sigma}{\partial \theta} = \frac{-\bar{R}T}{R_b(1-a\Gamma)} \frac{\partial \Gamma}{\partial \theta}. \quad (11)$$

8 The value of a (68 \AA^2) is obtained by fitting the equation 9 (solid line in Fig. 2b) to the surface
 9 tension measurements plotted in Fig. 2b.

10 Once the value of a is known, the surface concentration can be calculated by discretizing the
 11 equation 11 along θ . Employing a forward differences approach yields

$$12 \quad (\theta_{i+1} - \theta_i)(a\Gamma_i - 1) \left(\frac{R_p \tau_i}{RT} \right) + \Gamma_i = \Gamma_{i+1}. \quad (12)$$

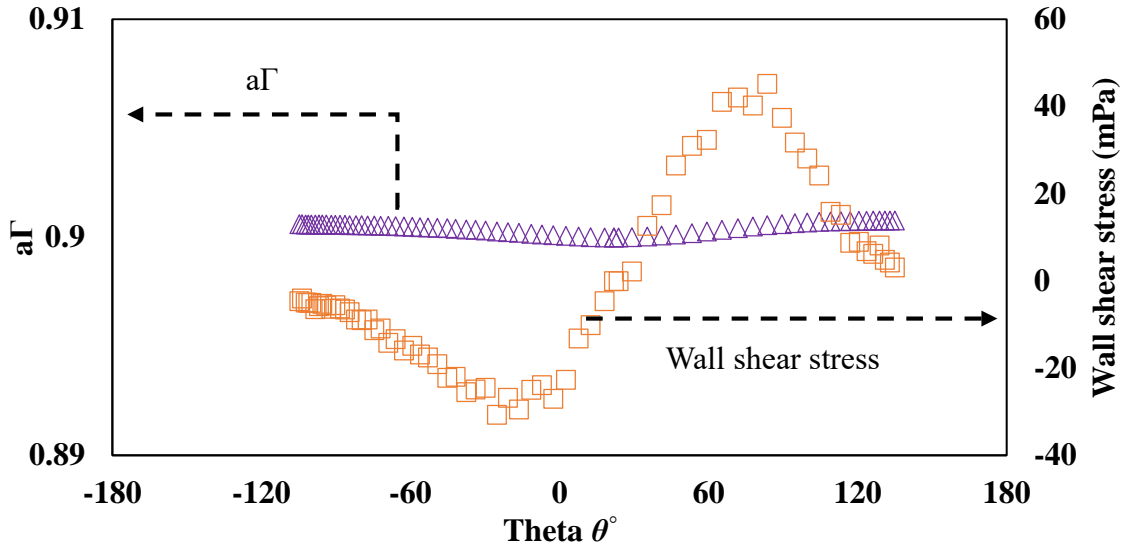


Figure 7. Hydrodynamic shear stress (orange squares) and surfactant distribution (purple triangles) calculated from experimental velocity measurements using equation 7 and 12.

13 Since the surfactant concentration in the shown measurements was around CMC , we estimate
 14 the interfacial concentration distribution for $a\Gamma = 0.9$ at the leading edge of the bubble (θ_1), i.e. we
 15 assume that 90% of the maximum concentration is reached there (note that this is just a hypothesis
 16 to illustrate the concentration distribution). As one can see from the calculations via equation 12,
 17 plotted in Fig. 7, the local surface coverage is only slightly modulated by the flow. This is due to
 18 the relatively small bulk velocity leading to stress magnitudes in the mPa range. Even minor surface
 19 tension gradients can compensate this weak shear. An example with distinct redistribution of the
 20 surfactant at higher bulk flow velocities is presented in the SI, Figure S3. However, the

1 hydrodynamic shear stress also shows that the conditions at the bubble in the asymmetric flow field
 2 essentially differ from the classical stagnant cap concept. In the symmetric flow case, the shear
 3 stress on the interface is free of curl and thus, can be compensated by Marangoni stress. However,
 4 the asymmetric shear has a rotational component ($\nabla \times \tau_m \neq 0$) that cannot be compensated by the
 5 Marangoni stress as Marangoni stress ($\tau_m \propto \nabla \Gamma$) results from the gradient of a scalar distribution
 6 (Γ) and thus, has to be free of curl ($\nabla \times \tau_m \propto \nabla \times \nabla \Gamma \equiv 0$). Hence, a rotational interfacial flow is
 7 induced in the asymmetric configuration and the adsorbed surfactant and PS particles are expected
 8 to circulate with the interfacial flow.

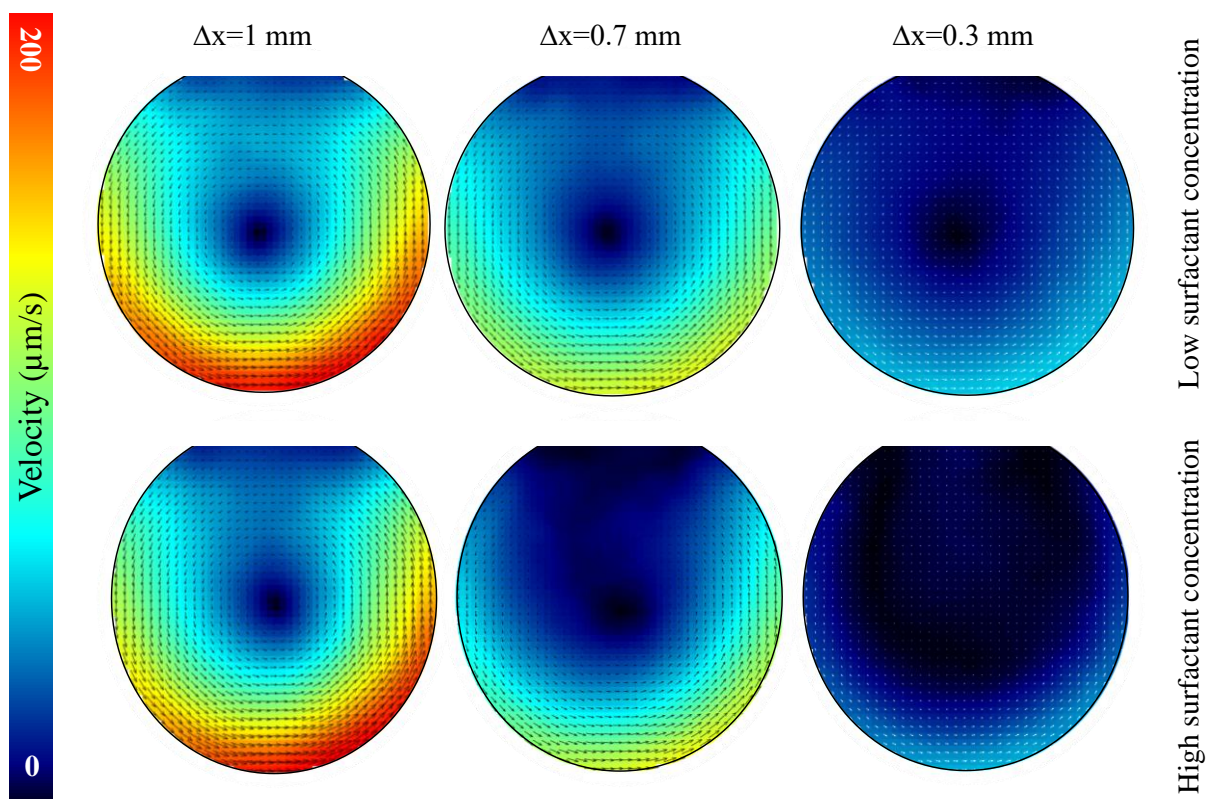


Figure 8. Circulating flow inside the droplet for different levels of asymmetry for 0.2 mM SDBS (upper) and 1.2 mM SDBS (lower) figures as measured by PIV.

9 3.5. Internal flow pattern for a liquid-liquid system

10 The flow pattern inside the air bubble cannot be resolved due to the experimental limitations
 11 associated with the tracer particle seeding in the gaseous phase. Hence, a liquid-liquid system was
 12 chosen to investigate the response of the interior fluid to the asymmetric flow field (video V3.mp4
 13 in SI). The experiments were repeated in the same geometrical configuration using the refractive
 14 index matching fluids discussed in Section 2.1. To that end, a water-glycol droplet containing the
 15 SDBS surfactant was submerged into the silicone oil. The PS particles were dispersed in the polar
 16 medium (water-glycerol droplet) and then the droplet was placed in the asymmetric shear flow,
 17 which again provides a defined asymmetric shear level on the droplet interface similar to the bubble
 18 case. Only due to the changed viscosities of the solutions, the Reynolds number and thus the flow

1 pattern differed from the bubble experiments. Fig. 8 shows the internal velocity field at center plane
2 i.e. $y=0$ depending on the degree of asymmetry for 0.2 mM SDSB and 1.2 mM SDBS. As it can be
3 seen from this figure, the internal circulation is intensified for both cases with growing shear rate.
4 For low surfactant concentration, higher velocity magnitudes are measured.

5 **Discussion**

6 To provide a sound interpretation of the described observations, we discuss the experimental
7 limitations, which typically have to be considered in the study of interfacial phenomena. Before
8 the flow measurements can be started, at least several minutes of waiting time are necessary to
9 attach enough PS particles at the interface for particle tracking. This can introduce impurities to
10 the system either from the surrounding atmosphere, construction parts, or due to the dissolution of
11 rhodamine which is contained in the PS particles. Consequently, this technique at its current stage
12 does not allow to investigate fresh and clean interfaces.

13 Furthermore, we note that the observed interfacial flow differs from the re-mobilization of the
14 interface at high surfactant concentration and fast sorption kinetics which is reported in ⁴⁷. This re-
15 mobilization happens when molecules freely desorb at the trailing edge and instantly adsorb at the
16 leading edge. Hence, if the surfactant mass transfer is fast enough, a uniform surface concentration
17 is obtained that is in equilibrium with the surrounding bulk phase. For bulk concentrations above
18 CMC, the existing micelles can provide the required permanent material exchange (given that the
19 kinetic processes are likewise fast enough). The resulting constant surface concentration excludes
20 Marangoni stresses and remobilizes the interface. This is contrasted by our observation of a no-slip
21 bubble surface and the downwards interfacial flow which opposes the upwards bulk flow.
22 Furthermore, the circulating interfacial flow also was observed at concentrations well below CMC,
23 which rejects the possibility of re-mobilization.

24 Additionally, we address the concentration dependence of the flow velocity observed for the case
25 of a liquid-liquid system. Unlike the bubble experiments, a decrease in magnitude of the internal
26 flow and thus the interfacial flow was obtained with increasing surfactant concentration. However,
27 higher surfactant concentrations also lead to a more elongated shape of the pendant drop which
28 interferes with the effect of the surfactant concentration on the surface velocity. For such elongated
29 shapes, the lateral extension of the drop is smaller and thus the shear rate decreases in comparison
30 to the low concentration case. Hence, to clearly analyze the effect of surfactant concentration on
31 the interfacial and internal flow, further extensive experiments are necessary, e.g. with different
32 surfactant types and buoyancy-matched phases.

33 Irrespective of these uncertainties, our experiments consistently show the existence of a
34 circulating interfacial flow under asymmetric shear. For the first time, we experimentally visualize
35 this phenomenon mainly known from theoretical studies before ^{28,48}. Our technique provides direct
36 access to the hydrodynamic behavior of the bubble surface by tracking the velocity of the attached
37 particles at the interface. This enabled us to reveal that the interface remains mobile even at high
38 surfactant concentrations and to distinguish the circulating interfacial flow from a pure solid body
39 rotation.

1 Based on the gained insights, Fig. 9 summarizes different scenarios for a surfactant-laden
 2 interface under dynamic conditions. For a rising bubble or a falling drop, the adsorbed material is
 3 swept to the trailing edge and the interfacial concentration at the leading edge decreases (Fig. 9a)
 4 ¹⁴. The attached bubble at a capillary needle that is placed in a perfectly symmetric flow will behave
 5 similarly, i.e. the surfactant is swept upward and accumulates at the stagnation zone of the capillary
 6 (Fig. 9b). However, since minor deviations in the positioning of the bubble and the applied jet flow
 7 are always effective, this situation never was observed in our experiments. Only for a perfectly
 8 symmetric case, the resulting viscous stress on the interface is free of curl and can be fully
 9 compensated by Marangoni stresses. This symmetric case could then result in a vanishing
 10 interfacial velocity. The movement of adsorbed tracer particles under asymmetric shear shows that
 11 the response of the interface to the bulk flow leads to a continuous circulation of the bubble surface
 12 with a stagnant zone around the capillary (Fig. 9c). The rotational component of the shear flow at
 13 the bubble interface redistributes the surfactant, thereby remobilizing the interface ^{27,49,50}. In this
 14 case, a pronounced velocity gradient exists at the bubble surface with zero velocity near the
 15 capillary as seen in Fig. 6a. This distinguishes the interfacial flow under asymmetric shear from a
 16 solid body-like rotation, despite their visual resemblance. Fig. 9d schematically sketches the
 17 interfacial flow around the capillary from top view.

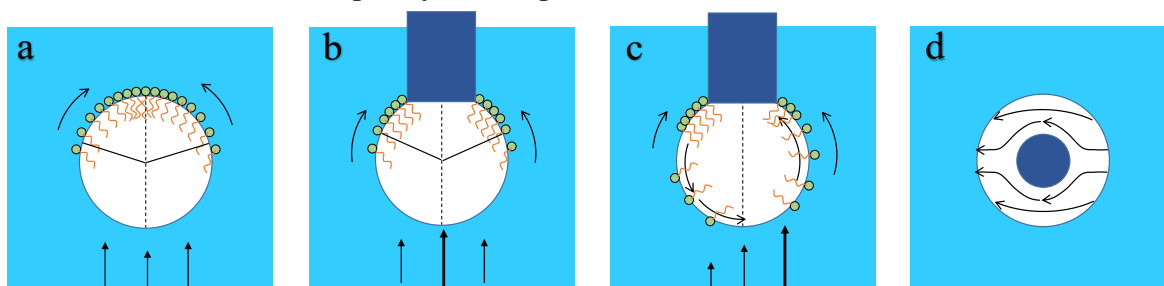


Figure 9. Schematic illustrating the surfactant distribution and shear forces for (a) a falling drop, (b) bubble in symmetric flow, (c) bubble in asymmetric flow in front view. (d) Flow field around the capillary in top view.

18 Conclusion and outlook

19 This study presents a direct experimental observation of the circulating interfacial flow ^{27,28,48–50}
 20 which occurs at a bubble under asymmetric shear flow in presence of the surfactant SDBS. Particle
 21 image velocimetry and particle tracking velocimetry (PIV/PTV) of adsorbed tracer particles is
 22 applied to investigate the flow structure and its magnitude. Extrapolation from bulk velocity
 23 measurements cannot fully capture the interfacial flow, which opposes the bulk flow on one side
 24 of the bubble, due to the limited spatial resolution and the high velocity gradients in the boundary
 25 layer. Instead, we tracked hydrophobic Polystyrene particles that are adsorbed directly at the
 26 interface of the bubble. Generally, for the tracking of adsorbed tracer particles, the influence of
 27 velocity gradients normal to the interface is restricted by the spatial extension of the particles, i.e.
 28 a few micrometers. Thus, our approach allows imaging the interfacial flow with sufficient
 29 accuracy.

30 A combined experimental and numerical characterization of the hydrodynamic shear acting on
 31 the bubble surface in asymmetric flow underlines the differences to the interfacial dynamics of

1 bubbles rising in quiescent liquid. In the symmetric flow, the Marangoni stresses resulting from
2 the nonuniform distribution of the surfactants can counteract the viscous shear stress and cause
3 immobility of the interface^{2,51,52}. Under asymmetric shear flow, the interface remains mobile even
4 at high surfactant concentrations. This impacts the interaction between the bubble surface and
5 approaching or detaching bubbles or particles in technological applications⁵³. Furthermore,
6 knowledge on the interfacial flow allows to better understand and control phenomena like lateral
7 bubble migration or the orientation of adsorbed anisotropic material. Our insights further are
8 relevant for the modelling of adsorption-desorption processes, and general mass transfer operations
9 (e.g. for dissolving gas bubbles) which are affected by the interfacial flow. Asymmetric shear can
10 be caused by wall effects, interactions between the dispersed entities, or the flow structure of the
11 continuous phase. Since these conditions apply for various reactors, our findings are significant for
12 a broad range of applications in chemical and minerals engineering.

13 To approach the technological conditions, i.e. bubbles with Reynolds numbers in the order of
14 100 and higher, the interfacial particle tracking can be extended to rising or falling drops and
15 bubbles in asymmetric shear flow. This requires an advanced measurement strategy, e.g. a camera
16 moving with the rising bubble. If it is possible to perform bulk PIV measurements in parallel to
17 PTV in the interface, comprehensive information on the hydrodynamic behavior of the moving
18 bubbles and drops can be obtained. Further, our model configuration of a buoyant bubble (or a
19 pendant drop for the liquid-liquid case) can be adapted to a precisely symmetric flow configuration.
20 This could be achieved by employing a flow channel with a homogeneous flow field to eliminate
21 the influence of small misalignments and to provide higher flow rates.

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28 **Supplementary material**

29 Electronic supplementary information (ESI) available. The flow pattern is shown for different
30 concentration of SDBS. Additionally, the numerically calculated velocity distribution around the
31 attached bubble for the case of free slip is reported. Finally, the wall shear stress and surfactant
32 distribution for higher velocities are calculated numerically and plotted.

33 Videos showing the movement of PS particles at the bubble surface, the interfacial flow of the
34 bubble as well as the internal circulation of the drop under shear flow are available.

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