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# Charge Transfer Induced Inter-layer Exciton in MoSe<sub>2</sub>/2D perovskite Hybrid Heterostructures

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## Abstract

Van der Waals crystals have opened a new and exciting chapter in heterostructure research, removing lattice matching constraints characteristic of epitaxial semiconductors. They provide unprecedented flexibility for heterostructure design. Combining two-dimensional (2D) perovskites with other 2D materials, in particular transition metal dichalcogenides (TMDs) has recently emerged as an intriguing way to design hybrid opto-electronic devices. However, the excitation transfer mechanism be-

tween the layers (charge or energy transfer) remains to be elucidated. Here, we investigate PEA<sub>2</sub>PbI<sub>4</sub>/MoSe<sub>2</sub> and (BA)<sub>2</sub>PbI<sub>4</sub>/MoSe<sub>2</sub> heterostructures by combining optical spectroscopy and density functional theory (DFT) calculations. We show that the band alignment facilitates charge transfer. Namely, holes are transferred from the TMD to the 2D perovskite, while the electron transfer is blocked, resulting in the formation of inter-layer excitons. Moreover, we show that the energy transfer mechanism can be turned on by an appropri-

ate alignment of the excitonic states, providing a rule of thumb for the deterministic control of the excitation transfer mechanism in TMD/2D-perovskite heterostructures.

## Introduction

Over the past few decades, semiconductor heterostructures have opened a new chapter in material engineering,<sup>1-4</sup> becoming the heart of every-day opto-electronic devices,<sup>5</sup> while providing a rich playground for fundamental solid state physics research.<sup>6,7</sup> The recent rediscovery of layered materials has launched the new era of van der Waals heterostructures, propelled by their ease of fabrication,<sup>4,8</sup> and almost infinite choice of constituent layered materials, including semiconductors, metals, superconductors, isolators and topological systems.<sup>9-14</sup> In contrast to epitaxial semiconductors, the absence of lattice matching constraints, permits the stacking of an almost unlimited combination of mono and few layers 2D crystals to form heterostructures with new exotic properties.<sup>15-19</sup> Moreover, with simple fabrication technology,<sup>20-22</sup> it is possible to obtain atomically sharp interfaces, and the close proximity of the stacked layers. The band alignment of the layers, together with their spacing, can easily be controlled by the appropriate selection of materials<sup>23-26</sup> This, together with strong excitonic effects,<sup>27-30</sup> make van der Waals heterostructures a very attractive system to investigate charge transfer<sup>31,32</sup> and energy transfer<sup>14,25,26,33</sup> with a view to applications.<sup>34-36</sup>

Among semiconducting layered materials, two families have received particular attentions over the past few years. Namely, transition metal dichalcogenides (TMDs)<sup>27,37</sup> and 2D hybrid perovskites.<sup>38,39</sup> Their fascinating properties make these systems promising candidates for a new generations of opto-electronic and energy harvesting devices.<sup>39-41</sup> Combining these two families of van der Waals crystal, it is possible to produce a new type of hybrid heterostructure. The functional (carrier confining) layers of the hybrid structure are separated by an organic spacer which is an intrinsic part of

the 2D perovskites. Despite the rapidly growing interest in this type of heterostructures,<sup>42-46</sup> the excitation transfer mechanism remains to be elucidated. Even in the presence of the wide band gap organic spacer, both types of excitation transfer (*i.e.*, charge or energy transfer) are observed.<sup>42,47</sup> However, the research published to date does not provide general conclusions concerning which mechanism dominates, and whether this can be controlled. This information is of paramount importance if we are to develop deterministic device assembly strategies.

Here, we address this issue for PEPI/MoSe<sub>2</sub> and BAPI/MoSe<sub>2</sub> heterostructures, where PEPI is (PEA)<sub>2</sub>PbI<sub>4</sub>, PEA is phenylethylammonium, BAPI is (BA)<sub>2</sub>PbI<sub>4</sub> and BA is buthylammonium (both 2D perovskites are  $n = 1$  *i.e.* the inorganic slab thickens corresponds to single PbI<sub>6</sub> octahedral unit). This investigation, together with our previous work,<sup>48</sup> shows that an appropriate choice of the TMD and the 2D perovskite organic spacer indeed allows to control the excitation transfer mechanism between the layers. The character of excitation transfer depends on the energy matching of the excitonic states between the layers. These conclusions are supported by our experimental and theoretical work, providing for the first time a rule of thumb for the deterministic control of the excitation transfer mechanism in these hybrid heterostructures. Our investigation indicates that, in general, it is the valence band alignment which provide the required conditions for the charge transfer of a hole from the TMD to the perovskite, leading to the formation of an inter-layer excitonic state. At the same time, energy transfer (if present), should transfers excitation from the 2D perovskite to the TMD.

## Results

We have used optical spectroscopy to investigate PEPI/MoSe<sub>2</sub> and BAPI/MoSe<sub>2</sub> heterostructures imaged in Fig. 1 (a-b). Each heterostructure consists of a 2D Ruddlesden-Popper perovskite multi-layer placed on top of monolayer MoSe<sub>2</sub>. To obtain the best

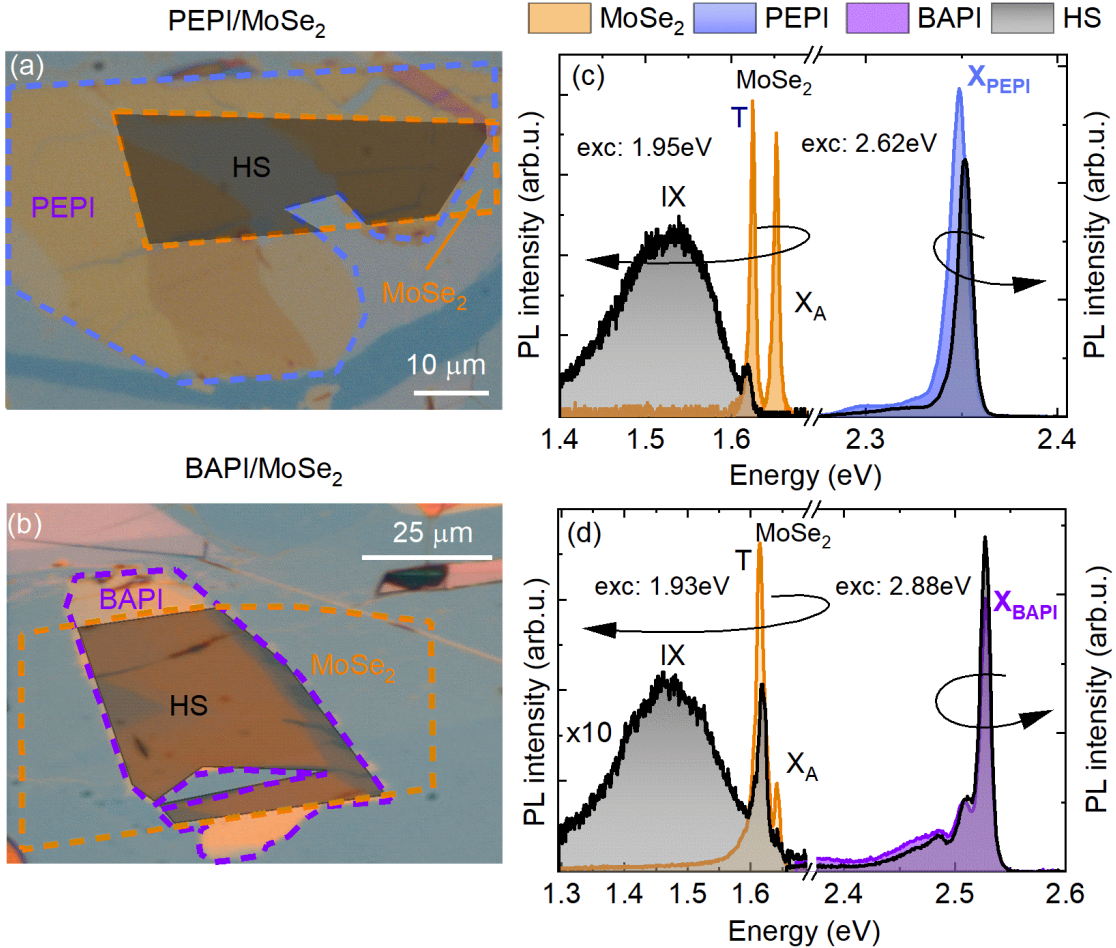


Figure 1: Optical microscope image of (a) PEPI/MoSe<sub>2</sub> and (b) BAPI/MoSe<sub>2</sub> structures. Blue (violet) dashed lines outline the edges of bare PEPI(BAPI), whereas orange dashed lines outline monolayer MoSe<sub>2</sub> flakes. The black shaded area indicates the heterostructure region. PL spectra measured on (c) PEPI/MoSe<sub>2</sub> and (d) BAPI/MoSe<sub>2</sub> heterostructures. In the heterostructure region an additional low energy (IX) peak is observed.

optical quality, provide environmental protection and stability under light illumination, the heterostructures are encapsulated in hexagonal boron nitride.<sup>49,50</sup> The resulting stacks are placed on a Si/SiO<sub>2</sub> substrate (for details see Methods section).

On the microscope images in Fig.1(a-b), regions of PEPI/BAPI are outlined by dashed blue/violet lines and the MoSe<sub>2</sub> monolayer regions are outlined by dashed orange lines. The heterostructure regions are indicated by a darker color where the TMD monolayer and the perovskite overlap. Each region has dimensions of a few microns to tens of microns, which is significantly larger than the spatial resolution of our micro-PL system. Therefore, an optical characterization can easily be performed for either the isolated layers or the heterostructure region.

The observed photoluminescence (PL) spectra of both samples, performed at 5 K are presented in Fig.1 (c-d). To separate the PL response for the different layers, we use lasers with different photon energies. To investigate the PL response from the TMD below 1.7 eV we use 633 nm laser light (1.95 eV) or 640 nm laser light (1.93 eV). This is below the absorption edge of the perovskites, thus avoiding emission from 2D perovskites defects or self-trapped excitons<sup>51</sup>. To excite the PEPI and BAPI layers we use above band gap laser light, above 2.2 eV (473 nm or 430 nm).

The PL emission from the isolated MoSe<sub>2</sub> monolayer and 2D perovskite regions are typical for these materials. Two PL peaks, at 1.65 eV and 1.62 eV (orange shading) related to monolayer MoSe<sub>2</sub> free exciton (X<sub>A</sub>) and negatively charged exciton/trion (T) recombination are

observed.<sup>52</sup> Similarly, for the isolated 2D perovskite regions, strong excitonic PL emission is observed at  $\sim 2.35$  eV for PEPI and  $\sim 2.53$  eV for BAPI, with characteristic low energy side bands.<sup>30,53,54</sup>

In the heterostructure regions a striking change in the PL spectra is observed for the TMD emission. A strongly broadened peak appears at lower energy (grey shading), which we assign to emission from the inter-layer exciton (IX) with the hole confined in PEPI or BAPI layer and electron in MoSe<sub>2</sub> (as we corroborate in the further parts of article). The maximum of this new PL emission is located at  $\sim 1.52$  eV for PEPI/MoSe<sub>2</sub> and at 1.47 eV for BAPI/MoSe<sub>2</sub>. Importantly, this new PL feature is observed only in heterostructure regions where the TMD and 2D perovskite layers are in contact. It is completely absent outside of the heterostructure region, as shown in spatially resolved PL maps in Fig.S1 (a-d). Our assignment of the IX transition is confirmed by photoluminescence excitation spectroscopy (see further part of the article) and the orders of magnitude longer PL decay time (see Fig. S2) than normally observed for TMDs<sup>55,56</sup> or 2D perovskite layers<sup>57,58</sup> at low temperature.

The appearance of the IX emission is accompanied by a strong decrease of the MoSe<sub>2</sub> excitonic emission (Fig.1(c-d)). For the PEPI/MoSe<sub>2</sub> heterostructure, the neutral exciton emission is completely quenched and the trion emission is around ten times lower. For BAPI/MoSe<sub>2</sub>, weak neutral exciton emission remains (seen as a shoulder) and trion emission is reduced by around 50% .

In both heterostructures, the intensity ratio between negative trion and  $X_A$  evidently rises indicating increasing n-type doping (in naturally n-type MoSe<sub>2</sub>). The increasing doping of MoSe<sub>2</sub> is additionally supported by reflectivity spectra, where the trion resonance appears only when TMD layer is in contact with the 2D perovskite (see Fig. S3). These results are indicative of an efficient charge transfer mechanism, where following the excitation, electrons remain in the MoSe<sub>2</sub> monolayer, while holes are transferred to perovskite layer, effectively increasing n-type doping of MoSe<sub>2</sub> and providing the re-

quired conditions for inter-layer exciton formation.

In contrast, changes in the PL corresponding to the perovskite emission are not so pronounced in the heterostructure region. Modifications of the PL intensity are rather moderate with a decrease in PEPI/MoSe<sub>2</sub> and increase in BAPI/MoSe<sub>2</sub>. Since the 2D perovskite multi-layers are much thicker, we expect charge transfer and energy transfer to have a relatively weak impact on the overall emission from the perovskite states due to the significant volume difference between the TMD and the perovskite layers.

Fig. 2 presents the results of DFT band structure calculations for both heterostructures. It is important to note that for the calculations the heterostructure was treated as an ensemble to correctly determine the band alignments<sup>48</sup> (see methods section and SI for more details regarding DFT computations). The TMD and 2D perovskite layers in both cases are incommensurate, thus, larger heterostructures with a twist angle were necessary in order to minimize the strain on the lattices below 0.2%. To reveal the contribution of particular orbitals to the valence and conduction bands we performed Mulliken analysis presented on the right hand side of panels (a) and (b). This shows that the top of the valence band in PEPI- and BAPI- heterostructure is mainly composed of orbitals from the PbI<sub>4</sub> slab, while the conduction bands edges are dominated by the TMD states, as clearly seen in the projected density of states (pDOS) plots. States related to the organic spacers are a few eV above the edges of lowest conduction bands (in both structures) forming barrier for electrons. Similarly in the valence band, the largest contribution of the organic spacer orbitals to the valence band DOS is observed at -6.5 eV and -7.8 eV, for PEPI/MoSe<sub>2</sub> and BAPI/MoSe<sub>2</sub> respectively, significantly below the top of the MoSe<sub>2</sub> and PbI<sub>4</sub> valence bands.

Closer inspection (expanded view of the top of the valence band), reveals a non-vanishing contribution of the organic spacers to the DOS between the valence band edges of PbI<sub>4</sub> and MoSe<sub>2</sub>. Consequently, a cascade-like band alignment is formed in the valence bands of



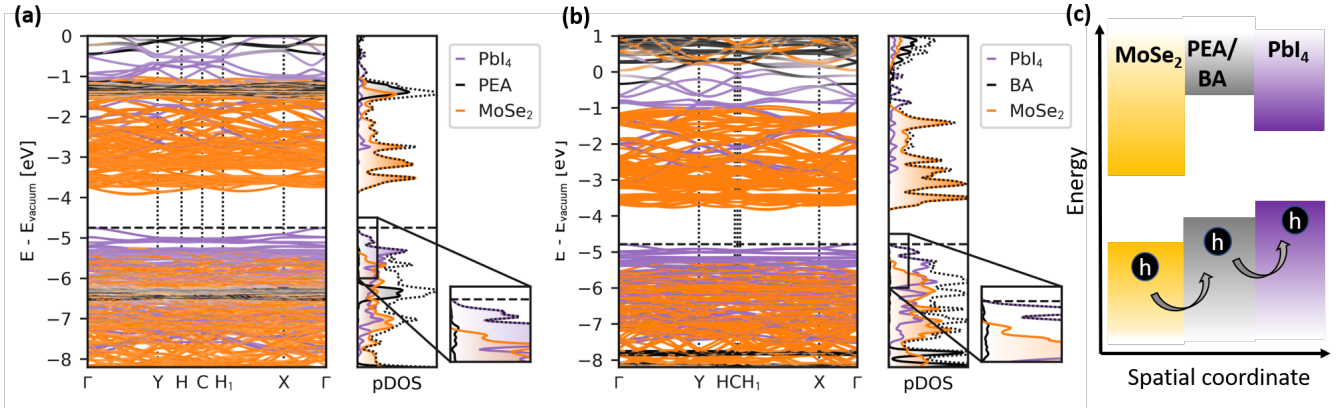


Figure 2: (a) and (b) Mulliken-projected band structure of the PEPI/MoSe<sub>2</sub> and BAPI/MoSe<sub>2</sub> heterostructure showing the majority contributions of each layer and density of states (pDOS) projected to particular building blocks (MoSe<sub>2</sub>, PEA or BA, PbI<sub>4</sub>). Zoom-in of pDOS shows contribution of organic spacer states between MoSe<sub>2</sub> and PbI<sub>4</sub> valence band edges. Both heterostructures indicate type-II band alignment. The valence band maximum (VBM) is localized in the PbI<sub>4</sub> layer at  $\Gamma$  point, while the conduction band minimum (CBM) is localized in the MoSe<sub>2</sub> layer at a low-symmetry  $k$  point between  $\Gamma$  and  $Y$ . (c) Schematic illustration of the band alignment in both heterostructures as calculated by DFT.

both heterostructures, facilitating hole transfer from MoSe<sub>2</sub> to the 2D perovskite, (as shown in panel (c) of Fig. 2), providing conditions for inter-layer exciton formation. Therefore, our DFT calculations support the hypothesis that the low energy PL originates from inter-layer exciton (IX) emission with the electron localized in the MoSe<sub>2</sub> layer and the hole localized in the 2D perovskite layer. Qualitatively, the same band alignment is observed for WS<sub>2</sub>/PEPI,<sup>48</sup> where an effective hole transfer is observed, however, there is no consensus concerning the existence of inter-layer emission in WS<sub>2</sub>/PEPI heterostructures.<sup>42,48</sup>

It is worth to note, that the energy of the valence band edge of PEPI and BAPI are at almost the same energy (according to our DFT calculation). Therefore, the gaps between conduction band edge of MoSe<sub>2</sub> and valence band edge of PbI<sub>4</sub> are almost the same in both heterostructures. This explains the small change in the energy of the IX emission, when PEPI is replaced by the higher band gap BAPI. Noteworthy, our single-particle DFT results account already for the main experimental observations, what implies that Coulomb corrections (typically obtained from GW or Bethe-Salpeter equation) should not contribute too much or would even cancel each other out.

Importantly, interlayer excitons appear prominently in PLE spectra as shown in Fig. 3(a-b). In both panels the integrated PL

intensities of T and IX are normalized to their intensity under the excitation wavelength corresponding to  $X_B$  resonance of MoSe<sub>2</sub>. For both heterostructures we observe an increase of the IX intensity when exciting in resonance with  $X_{\text{PEPI/BAPI}}$  (2.37/2.55 eV) or  $X_B$  in MoSe<sub>2</sub>. The enhancement of the IX PL emission observed for the resonant excitation with exciton states in either layer, strongly support the inter-layer nature of the IX emission. For example, even though the exciton resonance of PEPI does not correspond to any excitonic transition in MoSe<sub>2</sub>, an enhancement of the IX PL occurs, indicating that it is related to carriers (more specifically holes) created in the 2D perovskite layer. On the other hand, under resonant excitation with  $X_B$ , the particular band alignment favours hole transfer to PbI<sub>4</sub>, even if they are created in the MoSe<sub>2</sub> layer. Subsequently, Coulomb attraction between electrons in the MoSe<sub>2</sub> layer and holes in the 2D perovskite leads to the formation of inter-layer excitons.

The effective hole transfer from MoSe<sub>2</sub> to PbI<sub>4</sub> layer is further confirmed by the time resolved PL studies presented in Fig. 3(c-d). Even when the sample is excited with photon energy of 1.86 eV (significantly below 2D perovskites exciton states), the PL signal related to trion emission decays much faster in the heterostructure region (gray curves) than in bare MoSe<sub>2</sub> regions (orange curves). Therefore, the effective transfer of holes to the 2D perovskite

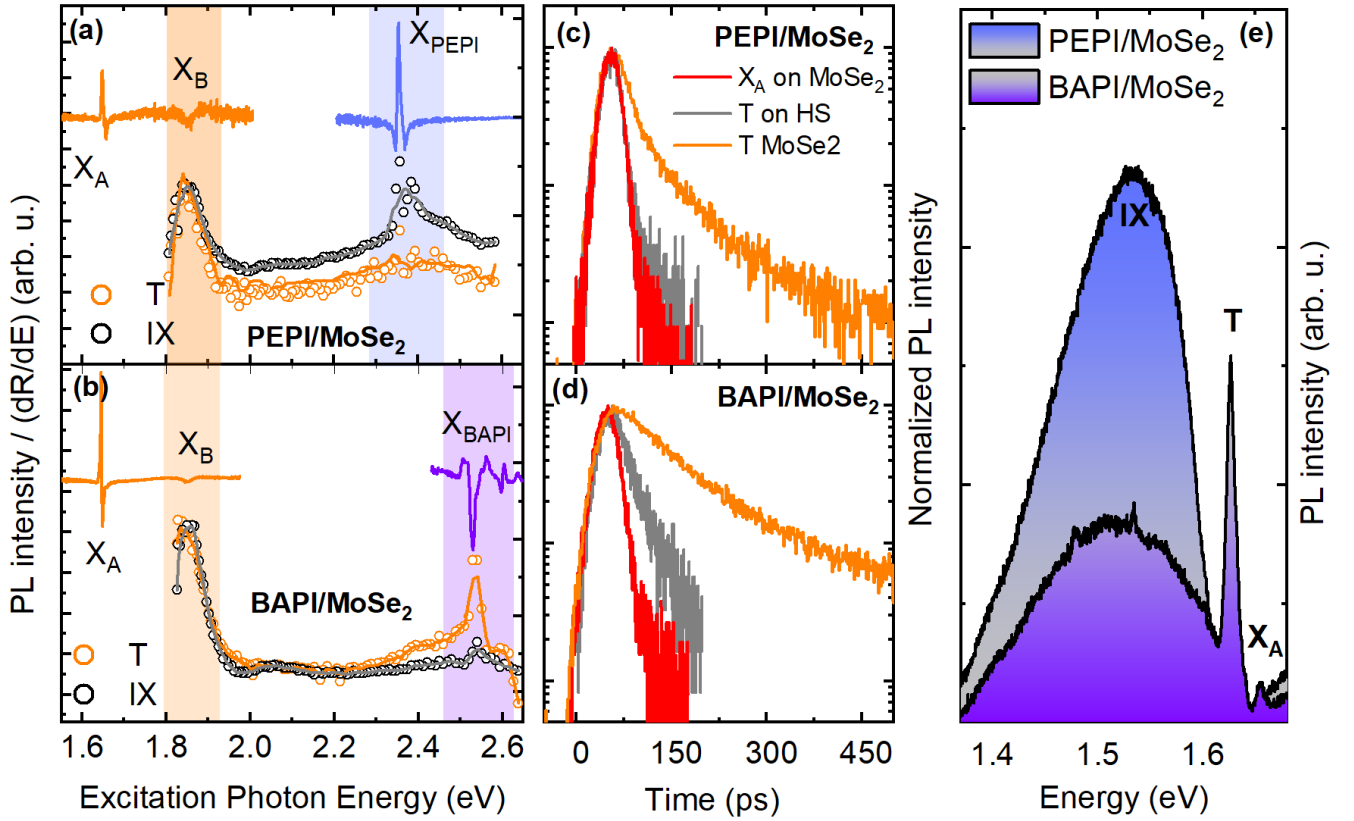


Figure 3: PL intensity versus excitation photon energy for (a) - PEPI/MoSe<sub>2</sub> and (b) - BAPI/MoSe<sub>2</sub> heterostructure. Integration was performed separately for T (orange) and IX (gray circles). The 1st derivative of reflectivity is also shown (orange solid lines for MoSe<sub>2</sub>, blue - PEPI and violet - BAPI), excitonic resonances of MoSe<sub>2</sub> (1.85 eV - X<sub>B</sub>) and 2D perovskites (2.35 eV - PEPI and 2.55 eV - BAPI) are clearly visible. PL decay curves for PEPI/MoSe<sub>2</sub> - (c) and BAPI/MoSe<sub>2</sub> - (d). Orange and red curves correspond to signal from T and X<sub>A</sub> on bare MoSe<sub>2</sub>, respectively, and grey curve - signal from T in the heterostructure region. (e) comparison of interlayer exciton PL intensity form PEPI/MoSe<sub>2</sub> and BAPI/MoSe<sub>2</sub>

layers increase the PL decay rate (which is sum of all process rates which decreases the trion population) corroborating our other experimental and theoretical results.

So far we have focused on the similarities between both heterostructures. However, some quantitative difference are seen which provide evidence for an energy transfer between the layers in BAPI/MoSe<sub>2</sub>. The first difference can be seen in the PLE dependence for the trion transition. While for PEPI/MoSe<sub>2</sub> there is almost no change of the trion intensity when exciting in X<sub>PEPI</sub> (orange circles in Fig. 3 (a)), a clear enhancement of the trion intensity is seen for BAPI/MoSe<sub>2</sub> (orange circles in Fig. 3 (b)). Since the calculated band structure exclude electron transfer to the MoSe<sub>2</sub> layers (or at least it has to be strongly suppressed), this enhancement has to be related to energy transfer from BAPI to MoSe<sub>2</sub>. The second and third

difference is presented in Fig. 3 (c,d,e). The trion emission in BAPI/MoSe<sub>2</sub> is longer than for the PEPI/MoSe<sub>2</sub> and IX emission is generally more intense for the PEPI/MoSe<sub>2</sub> compared to BAPI/MoSe<sub>2</sub> (under same excitation conditions) which may indicate a less effective hole transfer and/or an additional transfer process in the opposite direction, *i.e.* energy transfer from BAPI to MoSe<sub>2</sub>. Fig. 4 shows that the spectral overlap of different transitions in individual layers provides arguments that energy transfer indeed plays a role. Generally the X<sub>A</sub> and X<sub>B</sub> transitions in TMDs are significantly below the excitonic states of PEPI and BAPI. Only in the case of WS<sub>2</sub> the X<sub>B</sub> transition overlaps with PEPI excited exciton states (2s, 3s, ...) leading to previously reported Förster-like resonant (non-radiative) energy transfer.<sup>42,48</sup> According to the diagram, such a resonance can occur also for WS<sub>2</sub>/BAPI.

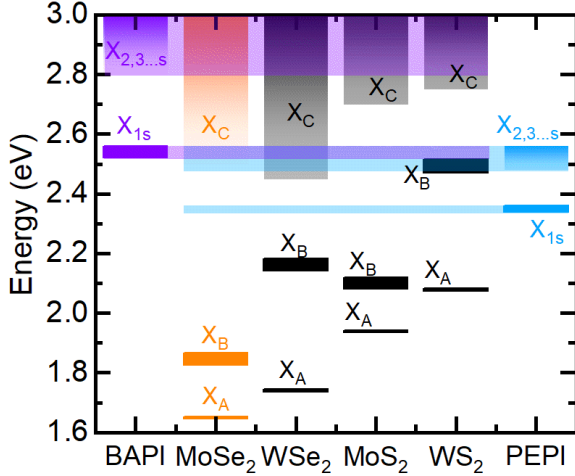


Figure 4: Diagram of excitonic transition energies at cryogenic temperatures in TMDs monolayers and  $(\text{BA})_2\text{PbI}_4$  (BAPI) and  $(\text{PEA})_2\text{PbI}_4$  (PEPI) 2D perovskites taken after. <sup>59,60,60–63</sup>

For the investigated heterostructures, the 2D perovskite exciton states overlap only with the onset of a broad TMD absorption feature referred to as the C exciton ( $X_C$ ).<sup>64–67</sup> For PEPI, the overlap occurs only for the excited exciton states and no energy transfer is observed. Crucially for BAPI, the overlap occurs for the 1s states, favoring energy transfer, which is observed as enhanced trion emission Fig.3 (b). This may indicate that the coupling of C excitation to PEPI exciton excited state is weak and Förster-like resonant energy transfer is suppressed in this case. In contrast the much higher oscillator strength of 1s transition in BAPI can enhance Förster coupling between the layers. Alternatively the experimental observation can also point that the energy transfer is mediated by photon reabsorption by the C exciton band. The 1s state of BAPI can effectively provide photons (to be absorbed by TMD layer) since it is the ground emissive state of the perovskite layer. In contrast, the exciton excited states in PEPI are poorly emissive due to the fast relaxation of excitons to the ground 1s state.

## Conclusions

We have reported a comprehensive investigation of charge and energy transfer in PEPI/MoSe<sub>2</sub> and BAPI/MoSe<sub>2</sub> hybrid het-

erostructures. We show that the excitation transfer in both heterostructures is dominated by charge transfer. Our DFT calculation shows that this is related to a cascade band alignment in the valence band of the heterostructure which facilitates hole transfer from MoSe<sub>2</sub> to the PbI<sub>4</sub> layer of the perovskite. The effective type II band alignment between MoSe<sub>2</sub> and the 2D perovskite gives rise to the formation of inter-layer excitons (IX), with PL emission below the intra-layer excitonic transitions. The inter-layer nature of the IX transition is supported by the long PL decay time and PLE studies. Moreover, for the case of BAPI/MoSe<sub>2</sub>, energy transfer is observed from the 2D perovskite to MoSe<sub>2</sub> monolayer. An analysis of the energies of excitonic transitions in the different layers which might indicate that energy transfer is related to reabsorption of photons in the MoSe<sub>2</sub> monolayer, which were emitted by the BAPI 1s ground state.

## Methods

### Synthesis and sample preparation

To obtain the hybrid samples we used the stamping technique established for inorganic 2D materials outlined in Ref.<sup>68</sup> Thin hBN flakes were first mechanically exfoliated on polydimethylsiloxane (PDMS) from bulk crystals (provided by T. Taniguchi and K. Watanabe, NIMS) and subsequently stamped on a 90°C preheated SiO<sub>2</sub>/Si substrate at ambient conditions. After annealing the hBN flakes at 180°C for 1-2 hours, similarly exfoliated monolayer MoSe<sub>2</sub> (bulk crystals from hqgraphene) are stamped on top of the hBN at a substrate temperature of 70°C and again annealed at 150°C. Single crystals of PEPI and BAPI were exfoliated and stamped using PDMS in the same way, but without the use of additional heating. The perovskite flakes were immediately fully encapsulated to inhibit degradation.

### DFT calculations

Model structures of MoSe<sub>2</sub>@(PEA)<sub>2</sub>PbI<sub>4</sub> and MoSe<sub>2</sub>@(BA)<sub>2</sub>PbI<sub>4</sub> were created using a coin-



cidence lattice algorithm implemented in hetero-builder<sup>69</sup> with less than 0.2 % strain on the individual layers. The  $\text{MoSe}_2@(\text{PEA})_2\text{PbI}_4$  heterostructure consists of 354 atoms and can be characterized by supercell vectors  $m_1 = (4, 1)$ ,  $m_2 = (-4, 5)$ ,  $n_1 = (-1, -1)$  and  $n_2 = (3, 0)$  with a rotation angle of  $\theta = 146.5^\circ$  and a vacuum spacing of 100 Å. The  $\text{MoSe}_2@(\text{BA})_2\text{PbI}_4$  heterostructure in the low-temperature phase consists of 207 atoms and can be characterized by supercell vectors  $m_1 = (-1, -4)$ ,  $m_2 = (4, 7)$ ,  $n_1 = (0, -1)$  and  $n_2 = (1, 2)$  with a rotation angle of  $\theta = 20.65^\circ$  and a vacuum spacing of 100 Å, see Ref.<sup>69</sup> for details (other representation choices are possible). These model structures were relaxed using FHI-aims<sup>70</sup> employing the PBE functional<sup>71</sup> on tight tier 1 numeric atom-centered orbitals, including the non-self-consistent Tkatchenko-Scheffler correction for dispersion interactions,<sup>72</sup> and scalar relativistic corrections (ZORA) on a  $2 \times 2 \times 1$   $\Gamma$ -centered  $k$ -grid. The  $\gamma$ -angle was kept fixed, while forces and stresses were minimized until below  $0.01 \text{ eV \AA}^{-1}$ . The SCF parameters were adjusted automatically after three steps. The electronic band structure, the Mulliken-projections, and the density of states were calculated including spin-orbit coupling (SOC) and considering the dipole correction on a  $4 \times 4 \times 1$   $\Gamma$ -centered  $k$ -grid.

## Optical measurements

The samples were mounted with the silver paste on the cold finger of a liquid helium-cooled optical cryostat. All the experiments were performed using a home-built setup at the temperature 5 K. The excitation source was halogen or xenon lamp (reflectivity), and continuous wave 633 nm laser diode, 640 nm solid state laser, 473 nm solid state laser, 400 nm pulsed laser diode, supercontinuum laser, second harmonic of a Ti:Sapphire laser or doubled frequency of optical parametric oscillator (PL). The light beam was focused on the sample with a spot of  $\simeq 1 \mu\text{m}$  diameter using a microscope objective with numerical aperture of 0.55 and magnification  $50\times$ . The same objective then collected the signal from the sample and di-

rected it to a 0.3 m or 0.5 m long spectrometer. A liquid nitrogen-cooled CCD camera was used as the signal detector. For PL measurements, the laser beam was filtered out by a long pass edge filter before entering the monochromator. Spatial PL mapping was performed with the scanning step  $1 \mu\text{m}$  along the  $x$  and  $y$  axes with the use of an automated  $xy$  translation stage on which the cryostat was mounted. PLE experiments were conducted using the same setup as the PL measurements. For time-resolved measurements the sample signal was detected by a single photon avalanche photo-diode with 1 ns setup time resolution (long time range) or streak camera with time resolution of 10 ps (short time range).

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