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Originally published:

February 2023

Nuclear Instruments and Methods in Physics Research A 1050(2023), 168125

DOI: <https://doi.org/10.1016/j.nima.2023.168125>

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1 **The application of encoder-decoder neural networks in high accuracy and efficiency**
2 **slit-scan emittance measurements**

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8

9 **Abstract**

10 A superconducting radio-frequency (SRF) photo injector is in operation at the electron linac
11 for beams with high brilliance and low emittance (ELBE) radiation center and generates
12 continuous wave (CW) electron beams with high average current and high brightness for user
13 operation since 2018. The speed of emittance measurement at the SRF gun beamline can be
14 increased by improving the slit-scan system, thus the measurement time for one phase space
15 mapping can be shortened from about 15 minutes to 90 seconds. The convolution neural
16 networks are applied to improve the efficiency and accuracy of beamlet images processing. In
17 order to estimate the uncertainty in the calculation of normalized emittance, we analyze the
18 main error contributions.
19

20 **1. Introduction**

21 High gradient radio-frequency photoelectron injectors (rf guns) are a kind of best candidates
22 to generate electron beams with low emittance, high brightness, and ultrashort bunches of pico-
23 to sub-picoseconds at present [1]. The remarkable high beam quality of these electron injectors
24 has opened up new development of modern accelerator-based scientific facilities, such as
25 extreme ultraviolet (XUV) [2,3] and X-ray free-electron lasers (X-FEL) [4], energy recovery
26 linacs (ERL) [5], MeV ultrafast electron diffraction (UED) [6], and hadron-beam cooling [7].

27 One of the most critical parameters characterizing rf guns is the transverse emittance.
28 Originally, the transverse emittance is defined as the projected area occupied by the beam
29 particles on the two-dimensional phase space [8, 9] at a given position z along the beam axis.
30 The area calculation is difficult for particle distributions with vaguely defined boundaries, and
31 it requires further specifications. An alternative and widely used way to overcome this difficulty
32 is to adopt the concept of root-mean-square (RMS) emittance based on the second moments of
33 the particle distribution, proposed by Lapostolle [10] and Sacherer [11].

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34 How to measure the transverse emittance with high accuracy and speed is always an important
35 question, especially at a user facility where the time slot for the beam diagnostics is limited,
36 and the task should be routinely done by the shift staff. Several measurement methods are
37 popular at most facilities, for instance, multi-screen method [12], quadrupole or solenoid scan
38 [13], beam tomography [14], slit-scan and pepper-pot [15]. An essential factor for selecting a
39 suitable method is based on whether the beam is emittance or space-charge dominated. A
40 criterion is defined in ref. [16]. For the low energy, high brightness beams from photo injectors,
41 the space charge contributes so considerably that such methods like slit-scan or pepper-pot
42 methods should be applied.

43 At the electron linac for beams with high brilliance and low emittance (ELBE) radiation
44 center [17], a superconducting radio-frequency (SRF) gun has been developed and operated as
45 an injector for the ELBE electron accelerator since 2007 [18]. At present, the SRF gun of second
46 generation is working, referred to as SRF gun-II. It includes a 3.5-cell 1.3-GHz superconducting
47 niobium cavity, a superconducting solenoid, and a photocathode with a corresponding laser
48 system. A cathode supporting system cooled with liquid nitrogen (LN₂) allows the operation of
49 normal-conducting photocathodes with a high quantum efficiency (QE). The SRF gun operates
50 in continuous wave (CW) mode with a repetition rate up to 13 MHz. A diagnostics beamline
51 allows the detailed characterization of the electron beam and the further optimization of the
52 SRF gun's operation.

53 To meet the requirement of emittance measurement in our user facility, i.e. speediness and
54 accuracy, we upgraded the slit-scan setup in the diagnostic beamline. The ultra-high-vacuum
55 (UHV) translation stage for the slit movement, drive motors, and control units have been
56 replaced by advanced systems. The slit moving velocity with the new motor is now adjustable
57 from 0 to 25 mm/s. The new control software has been developed, and the data analysis methods
58 have been improved meanwhile. The old beamlet images processing method we used was based
59 on 2D: first to use Gaussian fitting or set a threshold value to distinguish the beamlet and noise
60 images; second to filter and sum all beamlet images and scale the region-of-interest (ROI)
61 manually to avoid the influence from outside noise; third to calculate the emittance. However,
62 all the critical information for the phase space reconstruction and emittance calculation is the
63 beamlet projection profile in one dimension. Considering that machine learning (ML) has
64 become one of the most widely used and successfully developed method in image processing
65 [19], the benefits expected here for the data analysis of the slit-scan measurement are an
66 increase in speed, a higher accuracy of the beamlet profile, and the omission of manual
67 intervention during the image data processing.

68 In the first part of this paper, the theory of the slit-scan emittance measurement method is
 69 briefly reviewed. The second part describes the emittance measurement system in the SRF gun
 70 beamline. The third part introduces two convolutional neural networks (CNN) [19-21], whereby
 71 one is for beamlet images classification, and the other one, named encoder-decoder CNN, is for
 72 image noise reduction. The measurement error of the slit-scan process is discussed and analysed
 73 in the fourth part. Computer simulation of the slit-scan method based on the ASTRA code [22]
 74 is applied for the analysis in this part. The following fifth part presents our emittance
 75 measurement results with the new slit-scan system. The preciseness of the new measurement
 76 system is confirmed by comparing the experimental results with ASTRA beam dynamics
 77 simulation. The conclusions are given in the last part.

78

79 2. Slit-scan technique

80 2.1. Emittance measurement

81 The slit-scan and multi-slit techniques are widely used for measuring the transverse phase
 82 space and transverse projected emittance of high brightness electron beams produced by photo
 83 injectors. In these methods, the space charge dominated beam is split into many small and
 84 emittance dominated beamlets using a mask with one or several narrow slits. The particles of
 85 the beamlets drift from the mask position to a screen, as shown in Fig. 1. The data analysis
 86 works in the same way for single-slit scan as for multi-slit scan method. In both cases the
 87 particle divergence at slit position is transferred to a position distribution on the screen.

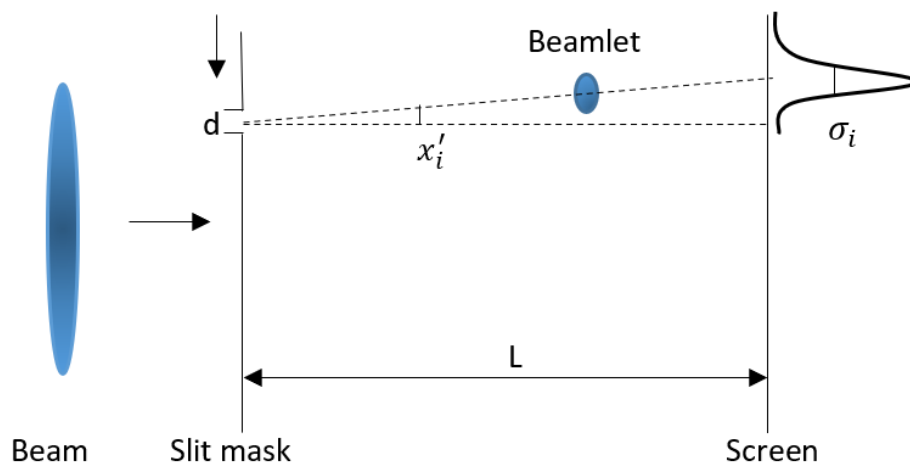


FIG. 1. Illustration of single-slit scan emittance measurement scheme.

88

89 For the beamlets a linear beam transport between the slit mask is assumed and thus the
 90 observation screen can be described by the transport matrix

$$\begin{pmatrix} x_{screen} \\ x'_{screen} \end{pmatrix} = \begin{pmatrix} 1 & L \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x_{slit} \\ x'_{slit} \end{pmatrix}. \quad (1)$$

The RMS transverse emittance ε is defined as

$$\varepsilon = \sqrt{\langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2}, \quad (2)$$

and a normalized transverse emittance ε_n can be written as

$$\varepsilon_n = \frac{p_z}{m_0 c} \sqrt{\langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2}. \quad (3)$$

Here the second moments $\langle x^2 \rangle$, $\langle x'^2 \rangle$, $\langle xx' \rangle$ are given based on the particle distribution $\rho(x, x')$:

$$\begin{aligned} \langle x^2 \rangle &= \int \rho \cdot (x - \langle x \rangle)^2 dx dx', \quad \langle x'^2 \rangle = \int \rho \cdot (x' - \langle x' \rangle)^2 dx dx', \\ \langle xx' \rangle &= \int \rho \cdot (x - \langle x \rangle)(x' - \langle x' \rangle) dx dx', \quad x' = \frac{p_x}{p_z}, \end{aligned} \quad (4)$$

where p_x is the horizontal beam momentum, p_z is the longitudinal beam momentum and it is approximately equal to the beam momentum, m_0 is the rest mass of electron, and c is the speed of light. In the slit-scan case, the $\langle \rangle$ is related to the averaging over the beamlets with the weight n_i , which are the particle intensities through the slit at i -th position. The bunch center at the slit plane is $\langle x \rangle = \frac{\sum n_i x_{si}}{\sum n_i}$, and x_{si} is the slit coordinate at i -th position. The beam size at the slit plane is $\langle x^2 \rangle = \frac{\sum n_i (x_{si} - \langle x \rangle)^2}{\sum n_i}$. The term $\langle x' \rangle = \frac{\sum n_i \bar{x}'_i}{\sum n_i}$ is the mean slope of the bunch with $\bar{x}'_i = \frac{\bar{x}_{sci} - x_{si}}{L}$. Here \bar{x}_{sci} is the position of the i -th beamlet center on the screen, and L is the drift

distance. The i -th beamlet divergence is $\sigma_i'^2 = \frac{\sigma_i^2 - \frac{d^2}{12}}{L^2}$, where σ_i is the i -th beamlet RMS size measured on the screen, d is the slit size and the factor $1/12$ is from the RMS value of the slit.

The quantities in Eq. (3) can now be expressed by values measured at the screen:

$$\langle x'^2 \rangle = \frac{\sum [n_i \sigma_i'^2 + n_i (\bar{x}'_i - \langle x' \rangle)^2]}{\sum n_i}, \quad (5)$$

$$\langle xx' \rangle = \frac{\sum n_i x_{si} \bar{x}'_i}{\sum n_i}. \quad (6)$$

2.2. Fast slit-scan measurement system at ELBE

The slit-scan system is a part of the diagnostics beamline, as shown in Fig. 2 [18]. The whole system is located at screen-station 2 and 3. Station 2 includes one single-slit mask with a 100 μm wide slit, one yttrium aluminum garnet (YAG) screen, and one calibration screen. Station 3 has one YAG screen, one optical transition radiation (OTR) screen, and one calibration screen (see Fig. 3). An encoder system delivers the actual slit position, and a second actuator serves for slit tilting with respect to the beam axis. Motor drivers and encoder electronics are made by Phytron GmbH. The distance between the slit mask and the YAG screen in screen-station 3 is 0.75 m. For image recording a 12-bit CCD camera Basler Scout with 659 x 494 pixels is used.

120 The corresponding size of one pixel on the screen is 25.3 μm . The control software is written
 121 in LabView and runs on a standard PC.

122 In the control software, the camera loop and the slit movement loop run in parallel, as shown
 123 in Fig. 4. The beamlet images are captured while the slit is continuously moving. In the i -th
 124 loop, the slit position P_{ci} is recorded, typically at 10 Hz depending on the macro pulse trigger
 125 which indicates that beam is on. At the same time T_{ci} , a command is sent to the camera to
 126 capture one image. During the camera exposure, the recording time is T_{ri} . The camera exposure
 127 time is usually chosen as long as the macro pulse length to cover the full pulse and to reduce
 128 the background noise from the dark current. Taking the aforementioned into account, the exact
 129 position of the slit when the camera captures the image can be written as

$$130 \quad P_{ri} = \frac{P_{ci+1} - P_{ci}}{T_{ci+1} - T_{ci}} \cdot (T_{ri} - T_{ci}) + P_{ci}. \quad (7)$$

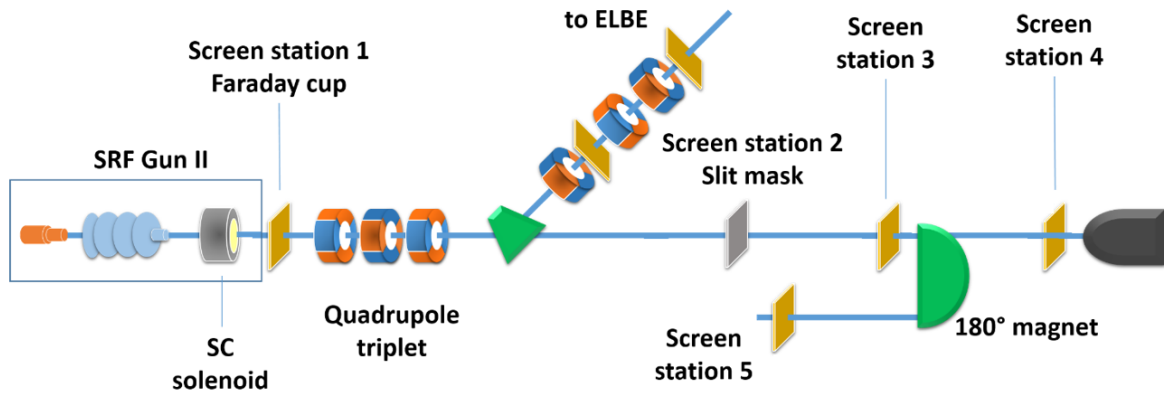


FIG. 2. The diagnostic beamline of ELBE SRF Gun II.

131

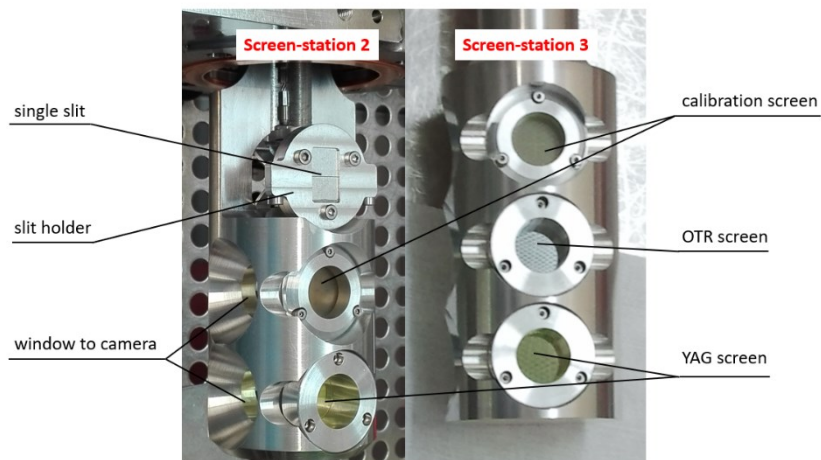


FIG. 3. Photographs of screen-station 2 and screen-station 3.

132

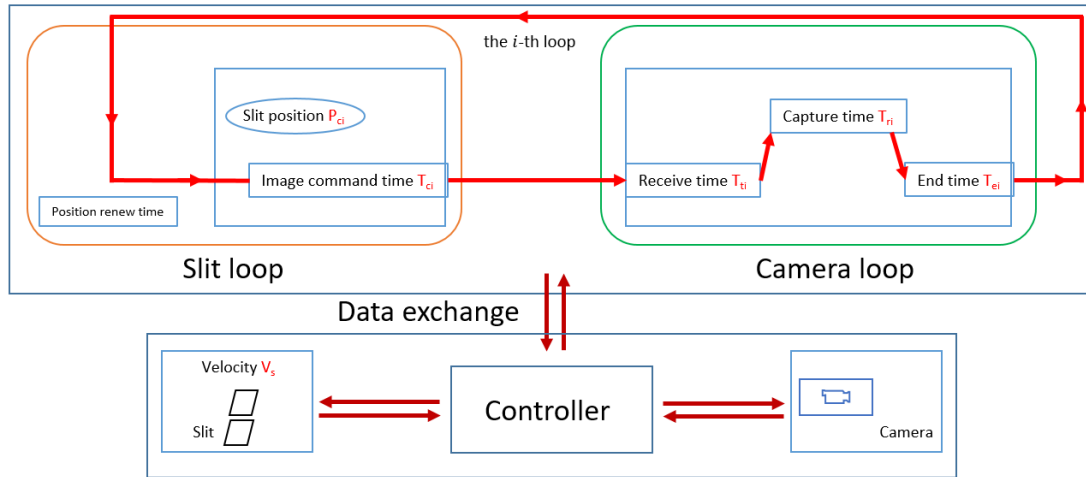


FIG. 4. Single-slit scan control system scheme.

133

134 3. Image processing based on Machine Learning

135 The first ML data processing step uses a CNN for image classification to eliminate datasets
 136 of needless images which contain no beamlet information. The input of the neural network is
 137 the horizontal projection of the beamlet images, which is a 1D intensity array with 494 values.
 138 The neural network structure is shown in Fig. 5 and consists of two convolution layers, where
 139 one pooling layer, and a fully-connected layer with two nodes as the output layer. The output
 140 is a one-hot encoding to determine the processing image is useful for further treatment.

141 The second image processing step is mainly intended for noise elimination. The input data is
 142 the 1D intensity array of the reduced number of beamlet image datasets selected in the first step.
 143 The output should be a nearly perfectly reconstructed beamlet intensity profile without noise
 144 and other artifacts. For that purpose, an encoder-decoder network is suitable [19]. The encoder-
 145 decoder consists of two parts, the encoder and the decoder. For the encoder part, the input is
 146 the data $x \in R^m$ and the output is the reconstructed data $y \in R^n$. One of the hidden layers stores
 147 the data features, written as the latent space h_k . The network has to learn the functions $f_e: R^m \rightarrow$
 148 R^k and $f_d: R^k \rightarrow R^n$. In principle, the features of the input data will be learnt and stored into the
 149 latent space, then the decoder layers will rebuild the signal as the output from the latent space.
 150 The specific structure of the encoder-decoder network used in this paper is presented in Fig. 6.

151

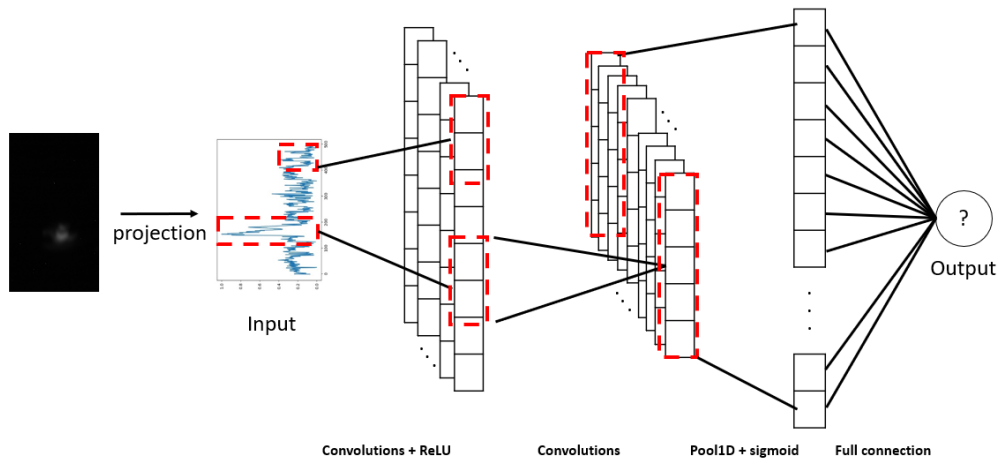


FIG. 5. Beamlet images classification network. The input data is a one-dimension signal with the beamlet intensity horizontal projection. The first convolution layer outputs 32 features with a leaky rectified-linear-unit (ReLU) function. The second convolution layer outputs 64 features. After this, a pooling layer and sigmoid function are used. The fully-connected layer is in the end and the log-softmax function scales the value from 0 to 1. The output value will be 1 when the log-softmax value between 0.5 and 1, and will be 0 otherwise.

152

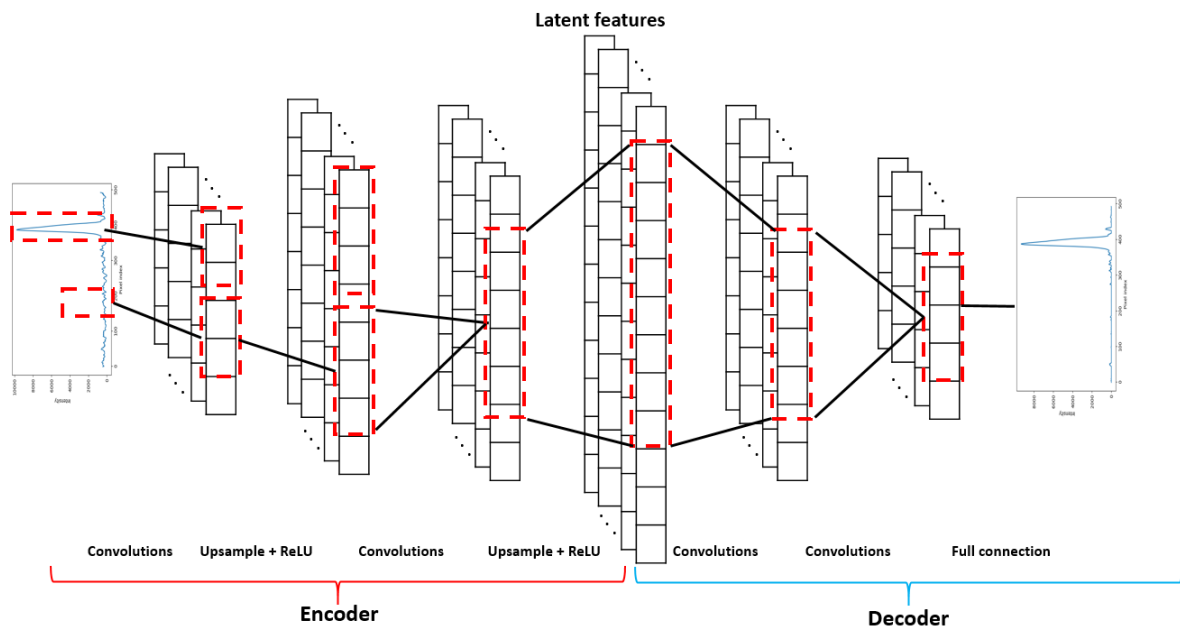


FIG. 6. The encoder-decoder network structures. The input data is the same as the classification network. The output features of the convolution layers in the encoder part are 16 and 32 with stride 1. The upsample layers are both nearest and scaling factors are 2. The latent features are 982. The output features of the convolution layers in the decoder part are 32 and 16 with stride 2. In the end is a full connected layer. The kernel sizes used are all 3. The total number of parameters is 2 005 887.

153

154 The ML networks have to be trained and tested. For the image classification network, 2500
 155 projection datasets from beamlet images were used, which were taken from experimental slit-
 156 scan measurements. Thereby 2000 were utilized for training and 500 for testing. The training
 157 applies the stochastic gradient descent method with the cross-entropy [23] as a loss function.

158 The final accuracy obtained from the test data is 98.8%. For the encoder-decoder network, the
159 training data came from 1502 experimental beamlet images processed manually and through
160 the median filter. Noise signal data was taken from 107 experimental images without beamlet
161 signals. Based on these, a random combination of filtered beamlet and noise data was used to
162 construct 167205 projection data records, of which, in turn 80% were used for training and 20%
163 for testing. Fig. 7 illustrates four examples of the dataset. The training procedure was performed
164 in the Maxwell Computer Cluster at DESY, using NVIDIA Tesla P100 GPU. The training time
165 was about one and a half hours with one thousand epochs, 3072 batch size and mean square
166 error (MSE) loss function. The optimizer used was Adam in Pytorch [24].

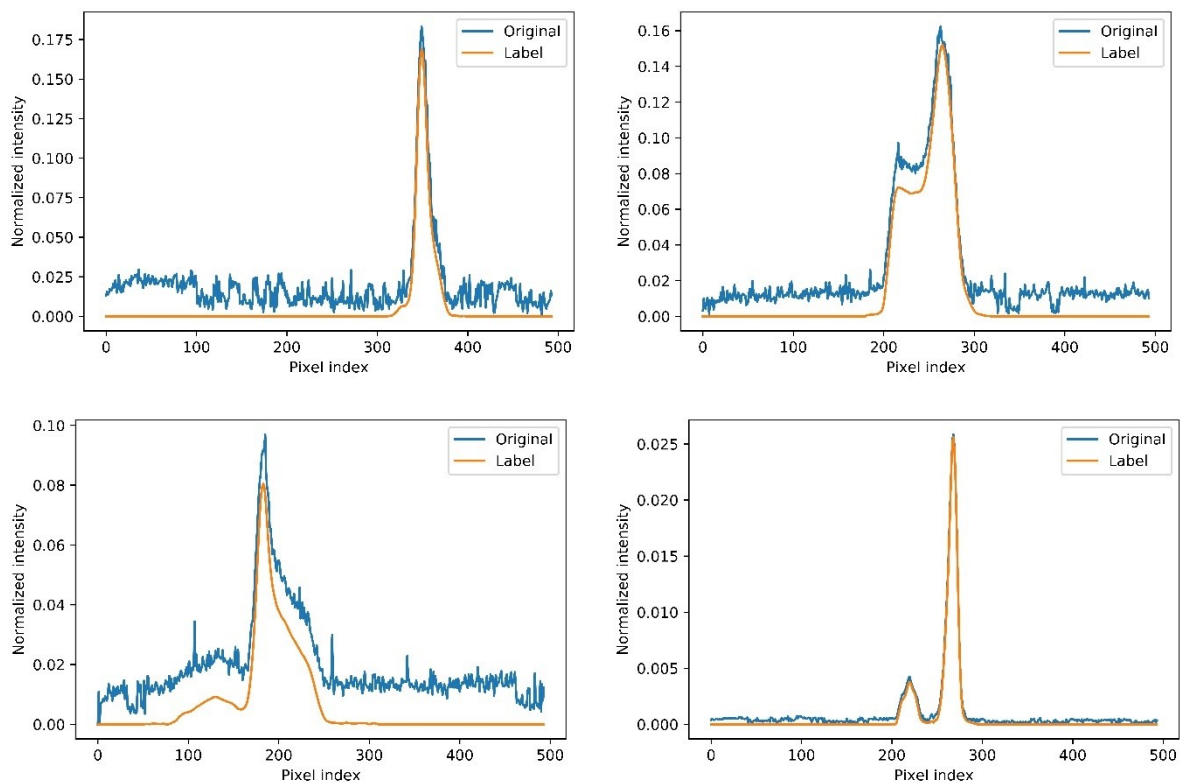


FIG. 7. The projection of beamlet images from simulation and the noise from the experiments.

167

168 Fig. 8 shows that the filter from machine learning (ML filter) has the potential to be more
169 accurate than traditional filters, such as median and Butterworth filters. The true signal profile
170 has two peaks with noise. The median and Butterworth filters can smooth the signal, but they
171 are helpless to depress the noise to a low level. The Gaussian fitting method distorts the signal
172 if it is beyond the Gaussian distribution. The advantage of the ML filter is, that it doesn't need
173 to adjust the parameters for different beamlet images once the neural network is well trained
174 and evaluated. The processing time for a single image is around 5 ms which is about one fourth
175 of the traditional processing method we use before.

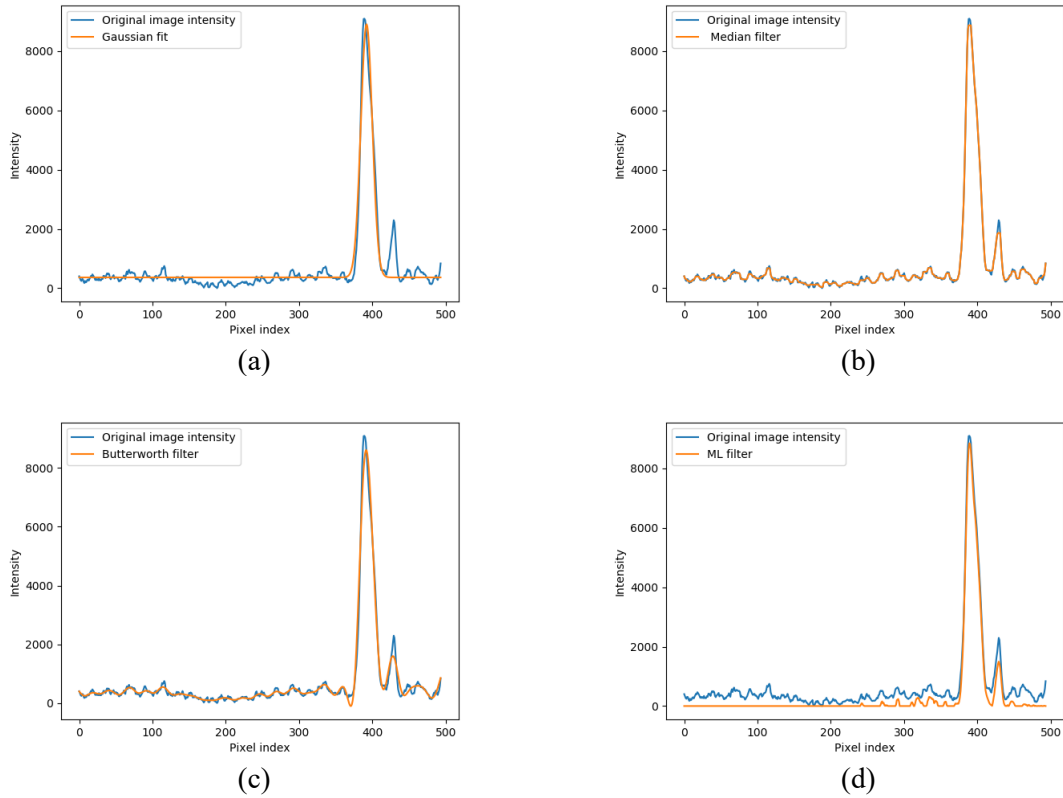


FIG. 8. One example of the comparison with different filters. (a) is Gaussian fitting; (b) is median filter with window length of seven; (c) is 5th order Butterworth filter and critical frequency of 0.09; (d) is ML filter.

176 Although the ML filter can reduce noise efficiently, the noise from dark current will influence
 177 the beamlet position and the RMS size calculation. The slit-scan can be done twice to mitigate
 178 this influence to some extent. The first scan is to measure the background from dark current,
 179 and the second scan includes beam and dark current. After subtracting the background, the
 180 further calculation of the beamlet center and RMS size are done twice. The first is by using the
 181 profile of the beamlet image. Then in the second calculation, only intensities in a certain range,
 182 beamlet center minus and plus f times RMS size from the first calculation, $[x_c - f\sigma_1, x_c +$
 183 $f\sigma_1]$, are considered. Usually, f is chosen between 0.5 to 5 depending on different image
 184 conditions. Fig. 9 and Tab. 1 show an example calculated with different f factors, which
 185 indicates that the beamlet RMS size is more sensitive to the value than the center position.

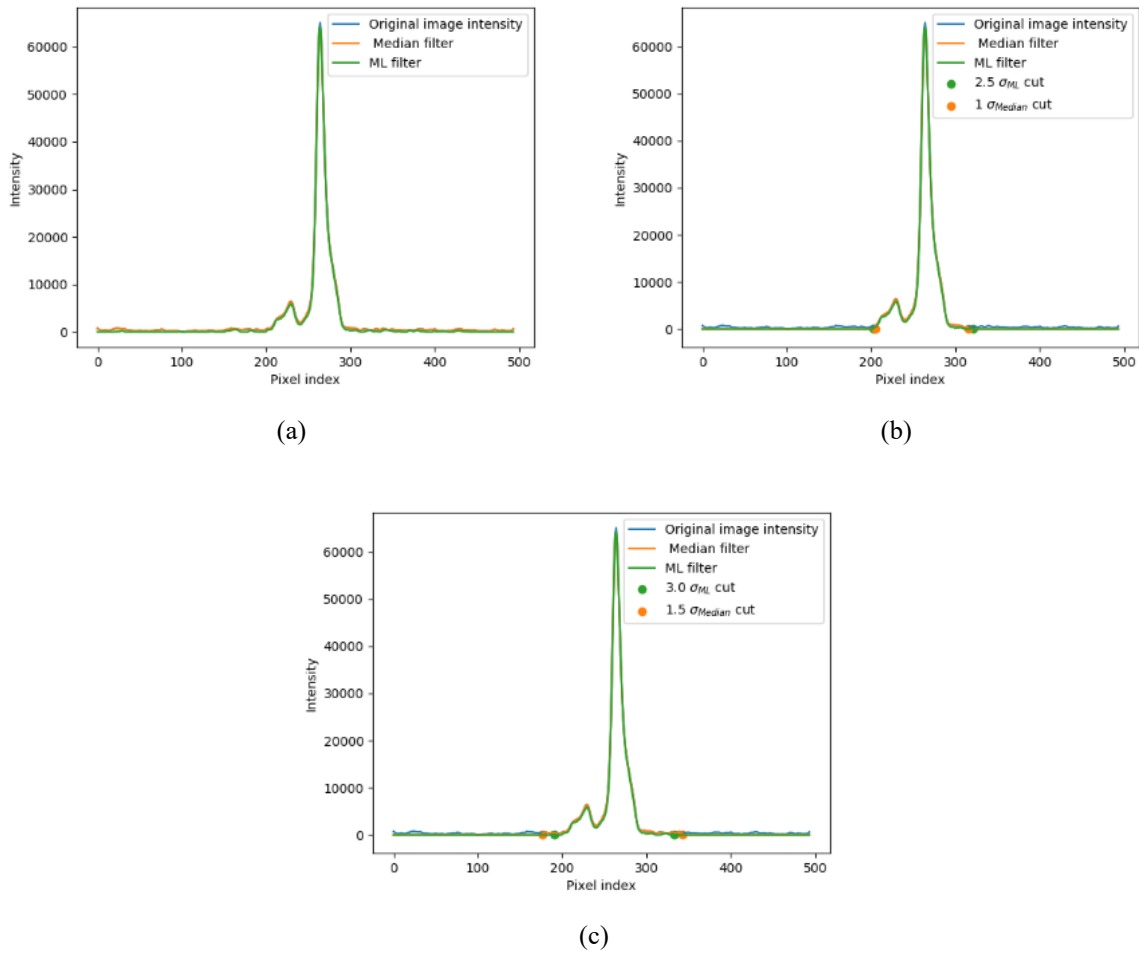


FIG. 9. One example with different cutting factors.

186

187

TAB. 1. Beamlets center, RMS size and intensity details of Fig. 10.

ML filter			Median filter		
Limit f	Center (pixel)	RMS size (pixel)	Limit f	Center (pixel)	RMS size (pixel)
no ¹	262.80	23.64	no ¹	260.58	55.07
2.5	262.40	15.36	1	262.29	16.15
3.0	262.50	15.71	1.5	262.31	19.29

188

4. Emittance correction factor and error analysis

189

4.1. Emittance correction factor

190

191 The beam RMS size can also be measured directly using the YAG screen at slit position.
 192 Measurement results showed that the reconstructed beam sizes obtained from the beamlet
 193 measurements are mostly smaller than the beam size directly measured on the screen at the slit
 194 position. The reason is the finite signal-to-noise ratio which causes signal losses at the low-

¹ means using the whole profile of the beamlet.

195 intensity edges of the beamlets. This effect has been identified for the first time at the PITZ
 196 photo injector [25], and a correction factor f_c has been introduced:

$$197 \quad f_c = \frac{\sigma_x}{\sqrt{\langle x^2 \rangle}}, \quad (8)$$

198 where σ_x is the beam RMS size measured at slit position, and $\langle x^2 \rangle$ is the second central moment
 199 of the beam distribution as determined by the slits-can measurement. Then the corrected
 200 normalized emittance can be written as

$$201 \quad \varepsilon_n = \frac{\sigma_x}{\sqrt{\langle x^2 \rangle}} \frac{p_z}{m_0 c} \sqrt{\langle x^2 \rangle \langle x'^2 \rangle - \langle x x' \rangle^2}. \quad (9)$$

202 This conservative approach of the slit-scan analysis has been used in this paper and belongs to
 203 the standard slit-scan procedure at the ELBE SRF gun beamline. Fig. 10 shows the correction
 204 factor as a function of the bunch charge. For low bunch charges, the factor is in some cases
 205 smaller than one. The reason is the dark current or image noise, which is not subtracted from
 206 the signal completely, and by that enlarging the reconstructed beam RMS size. In most cases,
 207 the factor is between 1.0 and 1.1, especially for higher bunch charges.

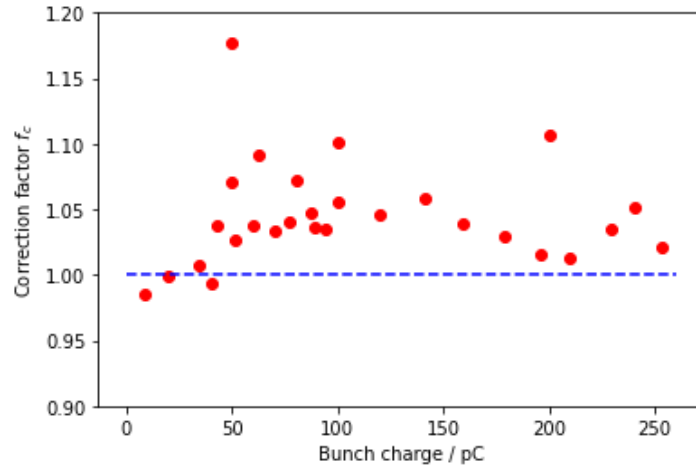


FIG. 10. Correction factor versus bunch charge. The blue dash line is equal to one and the red dots are the correction factors calculated from the slit-scan experiment at different bunch charges.

208 4.2. Error analysis

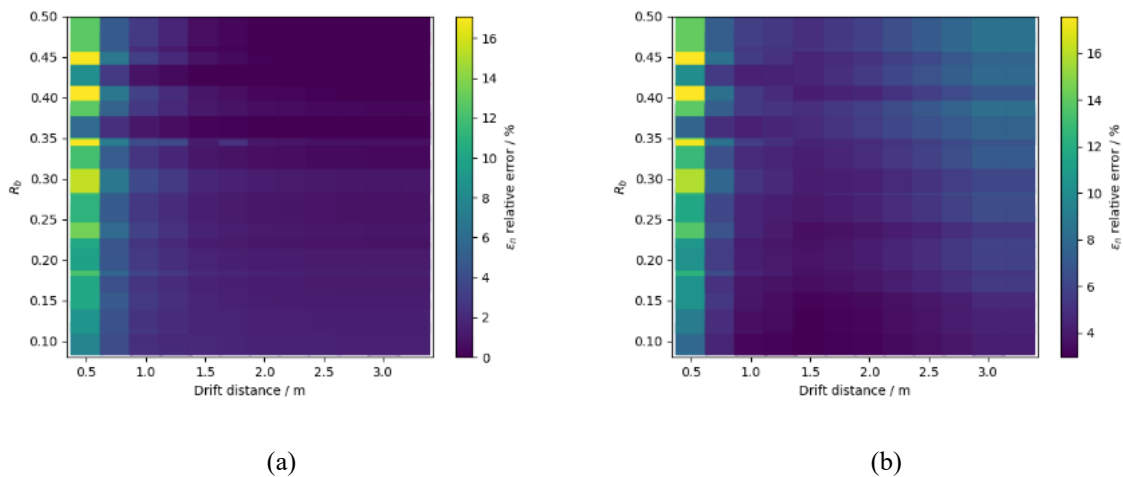
209 The accuracy of slit-scan emittance measurement is mainly determined by four sources: space
 210 charge influence in the beamlets (e_1), slit position recording error (e_2), uncertainties in the
 211 determination of the beamlet center position and RMS size (e_3), beam energy measurement
 212 uncertainly (e_4). The total relative error can be written as:

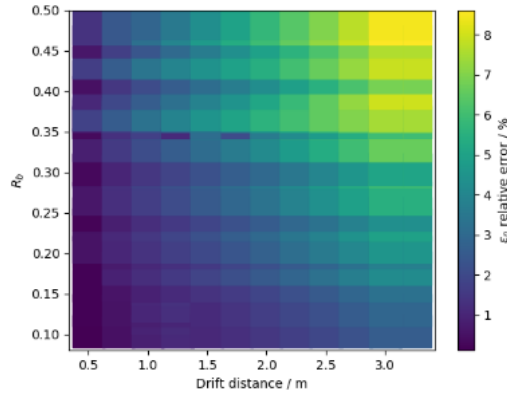
$$213 \quad e_t = \sqrt{e_1^2 + e_2^2 + e_3^2 + e_4^2} \quad (10)$$

214 Although the beam is divided into small slices which reduce the space charge force outside
 215 the slit width of the beam, if the beam density is large or the slit width is large, the beamlets
 216 may suffer from space charge force in the drift. Ref. [26] introduced a parameter based on the
 217 beam transverse envelope equation to evaluate the influence of the space charge force in slit-
 218 scan emittance measurements. Assuming that the beam distribution at the slit position is
 219 uniform and the slit width is d , the beamlet space charge dominance ratio is given by

$$220 \quad R_b = \sqrt{\frac{2}{3\pi}} \frac{I}{\gamma I_0} \left(\frac{d}{\varepsilon_n}\right)^2. \quad (11)$$

221 In this equation, ε_n is the normalized beam emittance, I is the beam peak current, and γ is the
 222 Lorentz factor representing the beam energy and I_0 gives the characteristic current as ec/r_e .
 223 When $R_b \ll 1$, the beamlet is emittance dominated and the influence of space charge is
 224 negligible. To evaluate the magnitude of the error from space charge, we have done some series
 225 of slit-scan simulations considering the influence of the drift distance and space charge. In the
 226 simulation, the slit width is $100 \mu\text{m}$ and the step width is fixed as $100 \mu\text{m}$, which can cover all
 227 beam without overlap. From the simulation results, the space charge and the drift distance cause
 228 errors in the emittance. Generally, when $R_b \leq 0.1$ and the drift distance is larger than 0.5 m , the
 229 error is less than 3% and will decrease with enlarging the drift distance, which is independent
 230 of space charge. For $R_b > 0.1$, the error from space charge increases with the drift distance
 231 enlarge, especially for large R_b , as shown in Fig. 11 (c).





(c)

FIG. 11. Slit-scan simulations: (a) without space charge, (b) with space charge, (c) pure space charge, from (b) subtracts (a).

232 However, R_b is related to beam current and emittance, which is from the bunch charge, length
 233 and horizontal size. In the simulations, we have changed the laser power, laser spot size on the
 234 cathode, gun phase and solenoid current that all determine the aforementioned beam parameters.
 235 Fig. 12 shows how R_b evolves with bunch charge for laser spot radii on the cathode of 1.25 mm
 236 and 1.875 mm. R_b at smaller laser spot radius on the cathode is larger than the bigger one for
 237 bunch charge less than 75 pC. For high bunch charge, larger than 100 pC, the smaller laser spot
 238 on the cathode has smaller R_b . When R_b is less than 0.5, the error is less than 10% at drift
 239 distance of 0.75 m from Fig. 11 (b).

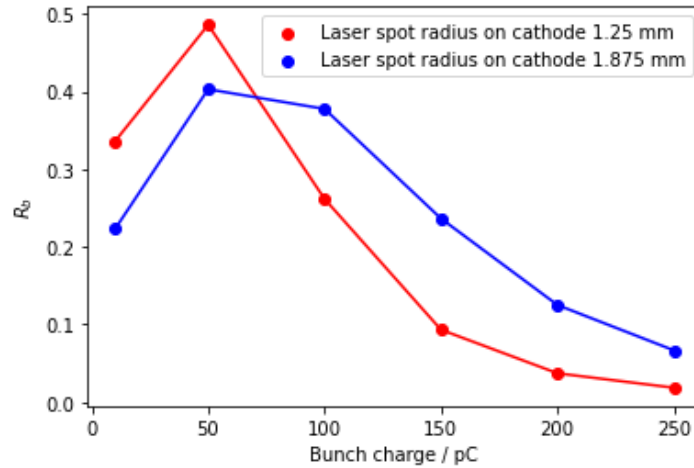


FIG. 12. R_b versus bunch charge for two different laser spot radii on the cathode.

240 In our equipment, the slit position recording uncertainty is less than 0.6% in average and the
 241 energy uncertainty is about 2%. These two factors are linear with the corresponding emittance
 242 relative error. Assume the averaged relative uncertainties of the beamlet intensity δ_n , the center
 243 position δ_c and the square of RMS size δ_σ , if they are independent for all beamlets and ignore
 244 the second and high order terms, the emittance relative error from these can be written as:

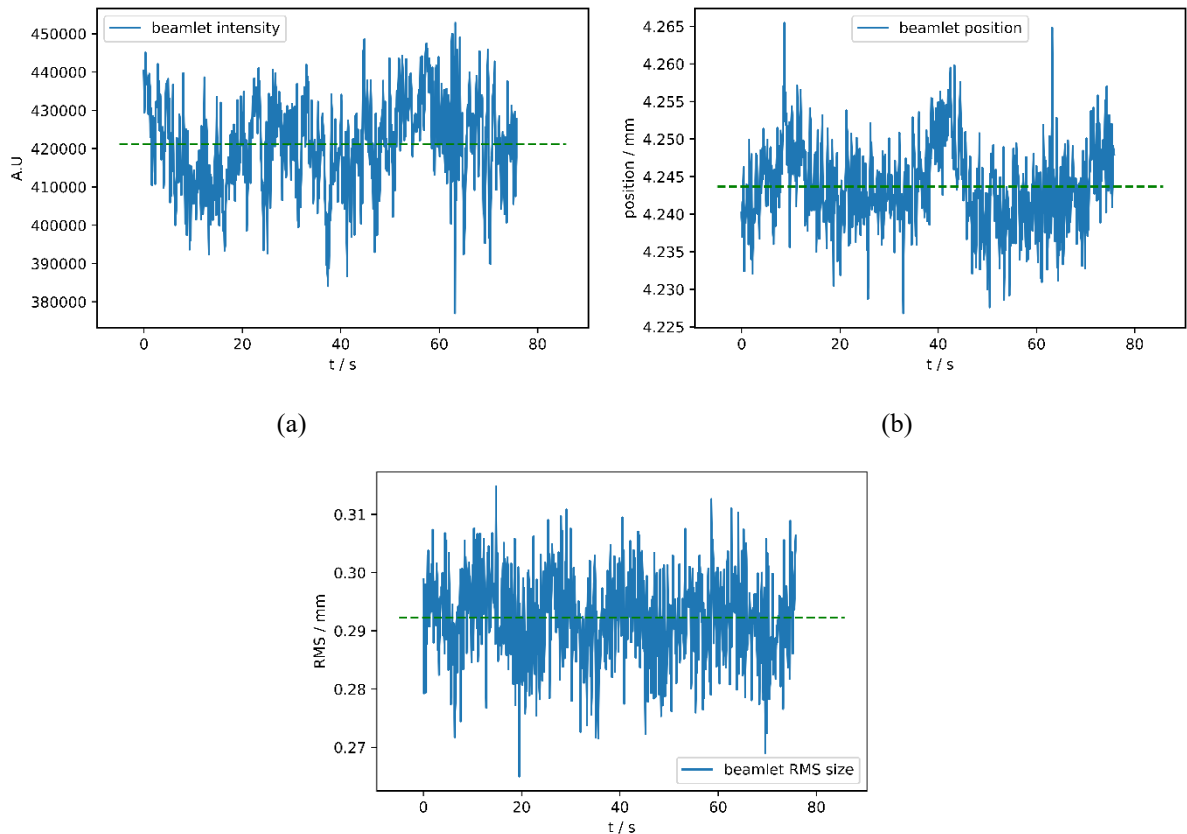
245
$$e_3 \approx \left| \delta_c + \delta_n + \frac{\delta_\sigma}{2} \right|. \quad (12)$$

246 The details about the derivation of this term are given in the Appendix A.

247

248 **5. Experiment results**

249 The experiments were carried out with beams of different bunch charges. The SRF gun
 250 gradient was set as 8.0 MV/m with a RF launch phase of 55°. The total energy of the beam was
 251 4.45 MeV. As discussed in the former section, to subtract the dark current, every slit-scan was
 252 repeated twice where one was without beam and the other one was with beam with the aim to
 253 subtract the dark current. The total measurement time was one and a half minutes. Tab. 2 shows
 254 the comparison of measurement results and the simulation. The errors are also list inside. The
 255 correction factor f_c was calculated by Eq. (8) and the influence of space charge, e_1 , was taken
 256 from the slit-scan simulation. The slit position uncertainty from the motor system was 0.2 %.
 257 The beamlet image intensity, center and RMS size uncertainties were mainly from the system
 258 jitter and image noise. In reality, the beamlet from the beam center was to be an evaluation of
 259 average of the whole beamlets. Fig.13 shows examples of beamlet intensity, center and RMS
 260 size fluctuations at the screen position. The energy uncertainty was around 2 % in our facility
 261 due to magnet calibration and RF launch phase drift. The total error, e_t , is calculated by Eq. (8).
 262 The normalized emittance for different bunch charges is shown in Fig. 14.



(c)

FIG. 13. Beamlet intensity, center and RMS size uncertainties. The green dash line is the average. The bunch charge is 50 pC and the beamlet is from the center of the beam. The uncertainties of beamlet intensity, center and RMS size are about 2.9%, 0.9% and 10%.

263

264 TAB. 2. Examples of measured normalized emittances, beam size correction factors f_c with ML filter,
 265 $f_{c,t}$ with traditional filter, charge percent and errors. σ_s and σ_e mean the beam RMS size at slit
 266 position in simulation and experiment. $\varepsilon_{n,s}$, $\varepsilon_{n,em}$ and $\varepsilon_{n,et}$ are the beam normalized emittance
 267 from the simulation, experiment with processing of ML filter and traditional filter,
 268 respectively.

Q (pC)	20	100	120	196	253
f_c	1.00	1.06	1.10	1.01	1.02
$f_{c,t}$	1.03	1.08	1.11	1.02	1.07
Charge percent	0.893	0.935	0.953	0.958	0.948
e_1 (%)	5	8	6	3	0
e_2 (%)	0.2	0.2	0.2	0.2	0.2
e_3 (%)	3.7	5	4.9	2.5	2.5
e_4 (%)	2	2	2	2	2
e_t (%)	6.54	9.64	8.00	4.39	3.21
σ_s (mm)	0.83	0.99	1.14	1.58	1.77
σ_e (mm)	0.93	1.28	1.46	1.64	1.73
$\varepsilon_{n,s}$ (mm·mrad)	1.46	2.84	3.10	4.55	6.04
$\varepsilon_{n,em}$ (mm·mrad)	1.80	3.65	3.42	5.12	6.19
$\varepsilon_{n,et}$ (mm·mrad)	2.5	4.92	4.12	5.23	6.37

269

270 As a comparison with normalized emittance from experiments, ASTRA simulations with
 271 different bunch charges were performed. The initial spatial beam distribution at the cathode is
 272 defined by two effects, the QE distribution of the cathode and the transversal intensity
 273 distribution of the laser. Two different emission conditions of the cathode have been appeared
 274 in the experiments, and are shown in Fig. 15. In the first row of Fig. 15, (a) shows an
 275 inhomogeneous QE map of the cathode. With the laser of 3.75 mm diameter with uniform
 276 distribution shown in (b), it generates a beam distribution as in (c), which is applied in the
 277 simulation with the results showing the red line in Fig. 14. With a smaller laser spot diameter
 278 of 2.5 mm, the homogenous part of the QE distribution could be selected and it produces a beam
 279 with Gaussian distribution like in Fig. 15 (f). In Fig. 14, the green line presents the emittance
 280 results of this situation. Fig. 15 (d) shows a well-distributed QE mapping from the experiment.

281 Together with a homogenous laser shape as in Fig. 15 (e), the beam at the cathode has then a
 282 Gaussian distribution. The cyan line in Fig. 14 is the result from this simulation with a Gaussian
 283 distribution beam. In simulation and experiments the temporal distribution of the laser was
 284 Gaussian with 2.3 ps RMS pulse length. The difference between the measurement results and
 285 the simulation is from the optical aberration, such as multipole fields parasitic in the solenoid
 286 or cavity [27]. Although we have installed the corrector including a normal quadrupole and a
 287 skew quadrupole, the influence of the unusual fields on the beam cannot be canceled totally.

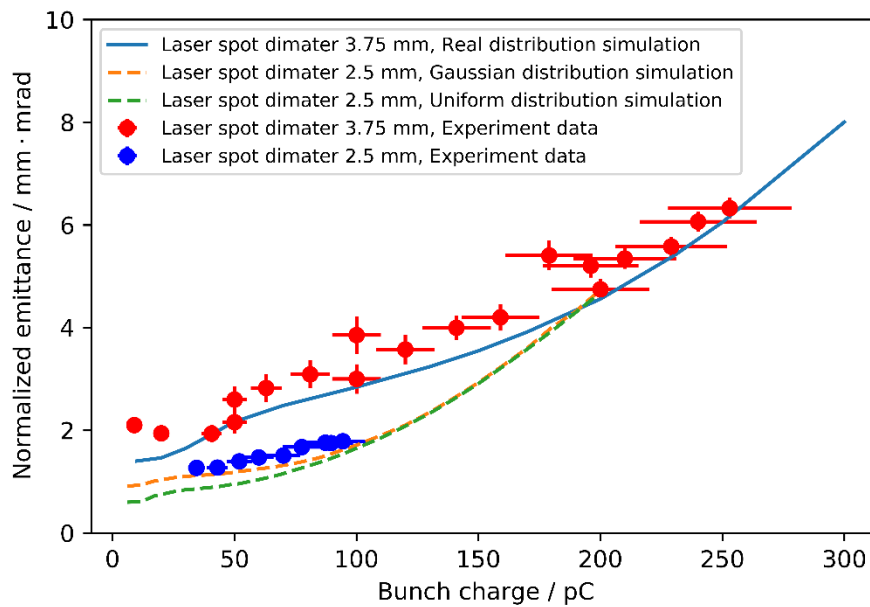
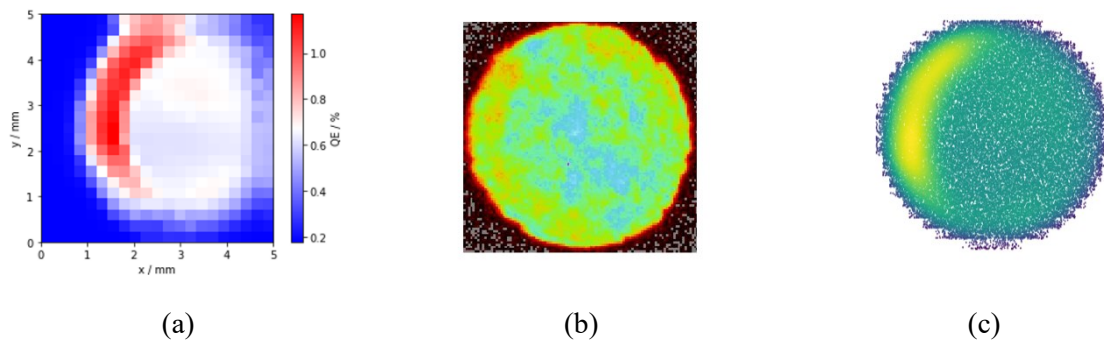


FIG. 14. Normalized emittance for varied bunch charges obtained from simulations and experiments with different spatial particle distributions at the cathode.

288



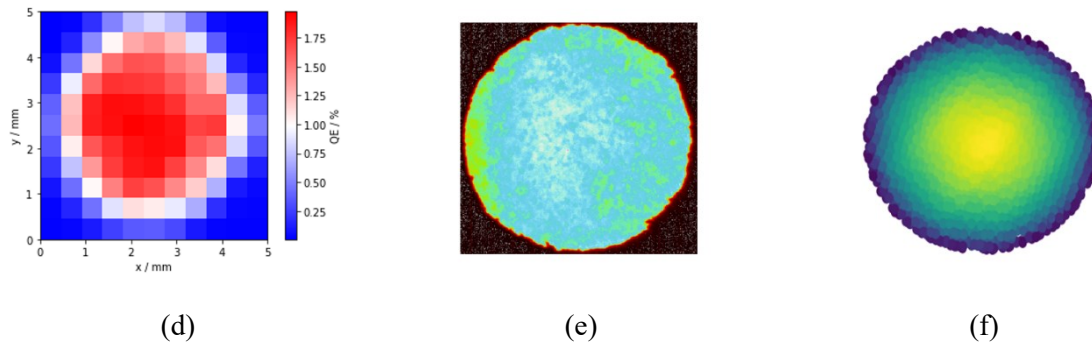


FIG. 15. (a) and (d) are the QE maps, (b) and (e) are the laser spot distributions on virtual cathode, (c) and (e) are original particles distributions in simulation. (c) is the inhomogeneous distribution and (f) is the gaussian distribution.

289

290

291 6. Conclusions

292 To improve the speed and the accuracy of the slit-scan emittance measurement at the ELBE
 293 SRF gun beamline, we constructed a new fast slit-scan system with a fast and continuous
 294 moving motor. Meanwhile, we have introduced two machine learning algorithms, the CNN for
 295 classification and the encoder-decoder CNN for filtering noise to shorten the image processing
 296 time. The ML filter is potentially more effective than the traditional imaging processing
 297 methods for beamlet images. The systematic errors from the slit moving and the image
 298 processing were attentively analyzed. At the end, the experimental measurement results were
 299 compared with the ASTRA simulations. The results confirmed the accuracy of the new slit-
 300 scan system besides the significant improvement of measurement speed.

301 Acknowledgement

302 We would like to thank the whole ELBE team for their help with the experiments. We also
 303 thank Dr. Houjun Qian from PITZ, DESY for his constructive discussions. This work was
 304 supported by China Scholarship Council and Chinese Academy of Engineering Physics. The
 305 machine learning part is supported by Helmholtz Information & Data Science Academy (HIDA)
 306 (No. 11952).

307

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- 377

378 **Appendix A**

379

380 Consider the averaged relative uncertainties of the beamlet intensity δ_n , the center position
 381 δ_c and the square of RMS size δ_σ . Assuming that they are independent for all beamlets, the i -
 382 th beamlet intensity, center and square RMS size can be written as

383
$$n_{i,r} = (1 \pm \delta_n)n_i, \quad (\text{A. 1})$$

384
$$\bar{x}_{sci,r} = (1 \pm \delta_c)\bar{x}_{sci}, \quad (\text{A. 2})$$

385
$$\sigma_{i,r}^2 = (1 \pm \delta_\sigma)\sigma_i^2, \quad (\text{A. 3})$$

386 where $\bar{x}_{sci,r}$ is the real center of the i -th beamlet on the screen. From these equations, $\langle x^2 \rangle_r$,
 387 $\langle x'^2 \rangle_r$ and $\langle xx' \rangle_r$ can be derived if we ignore higher order error terms:

388
$$\langle x^2 \rangle_r = \langle x^2 \rangle \pm \delta_n \langle x^2 \rangle, \quad (\text{A. 4})$$

389
$$\langle x'^2 \rangle_r = \langle x'^2 \rangle \pm \frac{2\delta_c}{L} \langle x \bar{x}_{sc} \rangle \pm \delta_\sigma \langle \sigma'^2 \rangle \pm \delta_n \langle x'^2 \rangle, \quad (\text{A. 5})$$

390
$$\langle xx' \rangle_r = \langle xx' \rangle \pm \frac{\delta_c}{L} \langle x_s \bar{x}_{sc} \rangle \pm \delta_n \langle xx' \rangle. \quad (\text{A. 6})$$

391 From the equations above, it can be seen that coordinate systems of the slit and screen position
 392 cross each other, when the beamlet center has an error. Ignoring higher orders of δ_n , δ_c , δ_σ , the
 393 calculated geometric emittance is

394
$$\varepsilon_c^2 \approx \varepsilon_0^2 \pm \frac{2\delta_c}{L} (\langle x^2 \rangle \langle x \bar{x}_{sc} \rangle - \langle xx' \rangle \langle x_s \bar{x}_{sc} \rangle) \pm \delta_\sigma \langle \sigma'^2 \rangle \langle x^2 \rangle \pm 2\delta_n \varepsilon_0^2. \quad (\text{A. 7})$$

395 Introducing

396
$$\frac{\langle x^2 \rangle \langle x \bar{x}_{sc} \rangle - \langle xx' \rangle \langle x_s \bar{x}_{sc} \rangle}{L} = k_c \varepsilon_0^2, \quad (\text{A. 8})$$

397
$$\langle \sigma'^2 \rangle \langle x^2 \rangle = k_\sigma \varepsilon_0^2, \quad (\text{A. 9})$$

398 then the emittance error from these uncertainties has the form

399
$$e_3 = \frac{|\varepsilon_c - \varepsilon_0|}{\varepsilon_0} \approx \left| \sqrt{1 \pm 2\delta_c k_c \pm 2\delta_n \pm \delta_\sigma k_\sigma} - 1 \right| \approx \left| \delta_c k_c + \delta_n + \frac{\delta_\sigma k_\sigma}{2} \right|, \quad (\text{A. 10})$$

400 Note that k_c and k_σ depend on the distribution of the beam in phase space and on the
 401 relationship of the coordinate systems at the slit and screen position. Practically it is difficult to
 402 calculate them because they include the geometric emittance true values. Here we estimate them
 403 to be the same magnitude as the true emittance and be one. By this simplification, the error
 404 from beamlet intensity, center position as well as RMS size uncertainties is written as

405
$$\left| \delta_n + \delta_c + \frac{\delta_\sigma}{2} \right|.$$